

TABLE 1-6 Relations between time-harmonic electromagnetic field and steady-state a.c. circuit theories

Field theory	Circuit theory
1. \mathbf{E} (electric field intensity)	1. v (voltage)
2. \mathbf{H} (magnetic field intensity)	2. i (current)
3. \mathbf{D} (electric flux density)	3. q_{ev} (electric charge density)
4. \mathbf{B} (magnetic flux density)	4. q_{mv} (magnetic charge density)
5. \mathbf{J} (electric current density)	5. i_e (electric current)
6. \mathbf{M} (magnetic current density)	6. i_m (magnetic current)
7. $\mathbf{J}_d = j\omega\epsilon\mathbf{E}$ (electric displacement current density)	7. $i = j\omega C v$ (current through a capacitor)
8. $\mathbf{M}_d = j\omega\mu\mathbf{H}$ (magnetic displacement current density)	8. $v = j\omega L i$ (voltage across an inductor)
9. <i>Constitutive relations</i>	9. <i>Element laws</i>
(a) $\mathbf{J}_c = \sigma\mathbf{E}$ (electric conduction current density)	(a) $i = G v = \frac{1}{R} v$ (Ohm's law)
(b) $\mathbf{D} = \epsilon\mathbf{E}$ (dielectric material)	(b) $Q_e = C v$ (charge in a capacitor)
(c) $\mathbf{B} = \mu\mathbf{H}$ (magnetic material)	(c) $\psi = L i$ (flux of an inductor)
10. $\oint_C \mathbf{E} \cdot d\mathbf{l} = -j\omega \iint_S \mathbf{B} \cdot d\mathbf{s}$ (Maxwell–Faraday equation)	10. $\sum v = -j\omega L_s i \simeq 0$ (Kirchhoff's voltage law)
11. $\iint_S \mathbf{J}_{ic} \cdot d\mathbf{s} = -j\omega \iiint_V q_{ev} dv = -\frac{\partial Q_e}{\partial t}$ (continuity equation)	11. $\sum i = -j\omega Q_e = -j\omega C_s v \simeq 0$ (Kirchhoff's current law)
12. <i>Power and energy densities</i>	12. <i>Power and energy</i> (v and i represent peak values)
(a) $\frac{1}{2} \iint_S (\mathbf{E} \times \mathbf{H}^*) \cdot d\mathbf{s}$ (complex power)	(a) $P = \frac{1}{2} v i$ (power-voltage-current relation)
(b) $\frac{1}{2} \iiint_V \sigma \mathbf{E} ^2 dv$ (dissipated real power)	(b) $P_d = \frac{1}{2} G v^2 = \frac{1}{2} \frac{v^2}{R}$ (power dissipated in a resistor)
(c) $\frac{1}{4} \iiint_V \epsilon \mathbf{E} ^2 dv$ (time-average electric stored energy)	(c) $\frac{1}{4} C v^2$ (energy stored in a capacitor)
(d) $\frac{1}{4} \iiint_V \mu \mathbf{H} ^2 dv$ (time-average magnetic stored energy)	(d) $\frac{1}{4} L i^2$ (energy stored in an inductor)

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