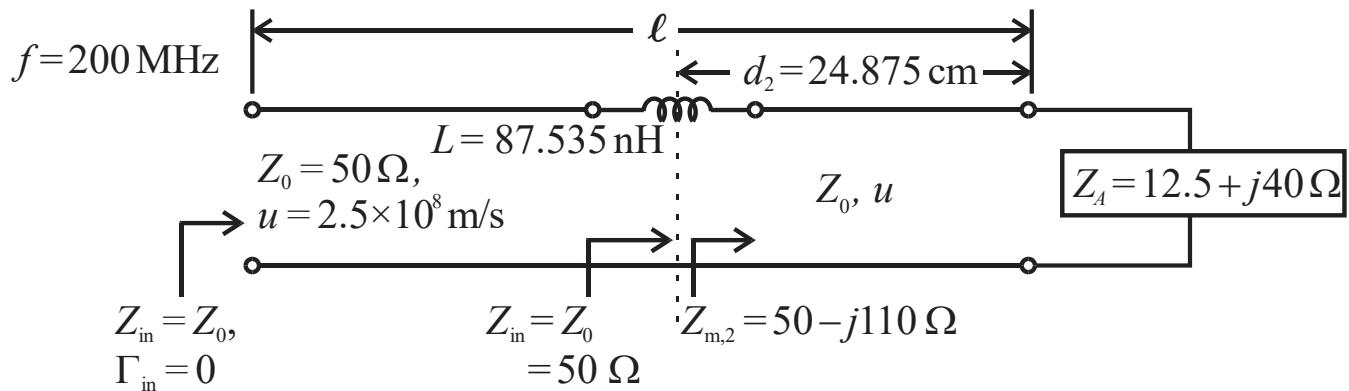


You have an antenna with input impedance  $Z_A = 12.5 + j40 \Omega$  at 200 MHz. Match it to a feeding transmission line ( $Z_0 = 50 \Omega$  &  $u = 2.5 \times 10^8 \text{ m/s}$ ) using a discrete inductor connected in series as close to the antenna as possible. Draw a fully labeled sketch of the final design.

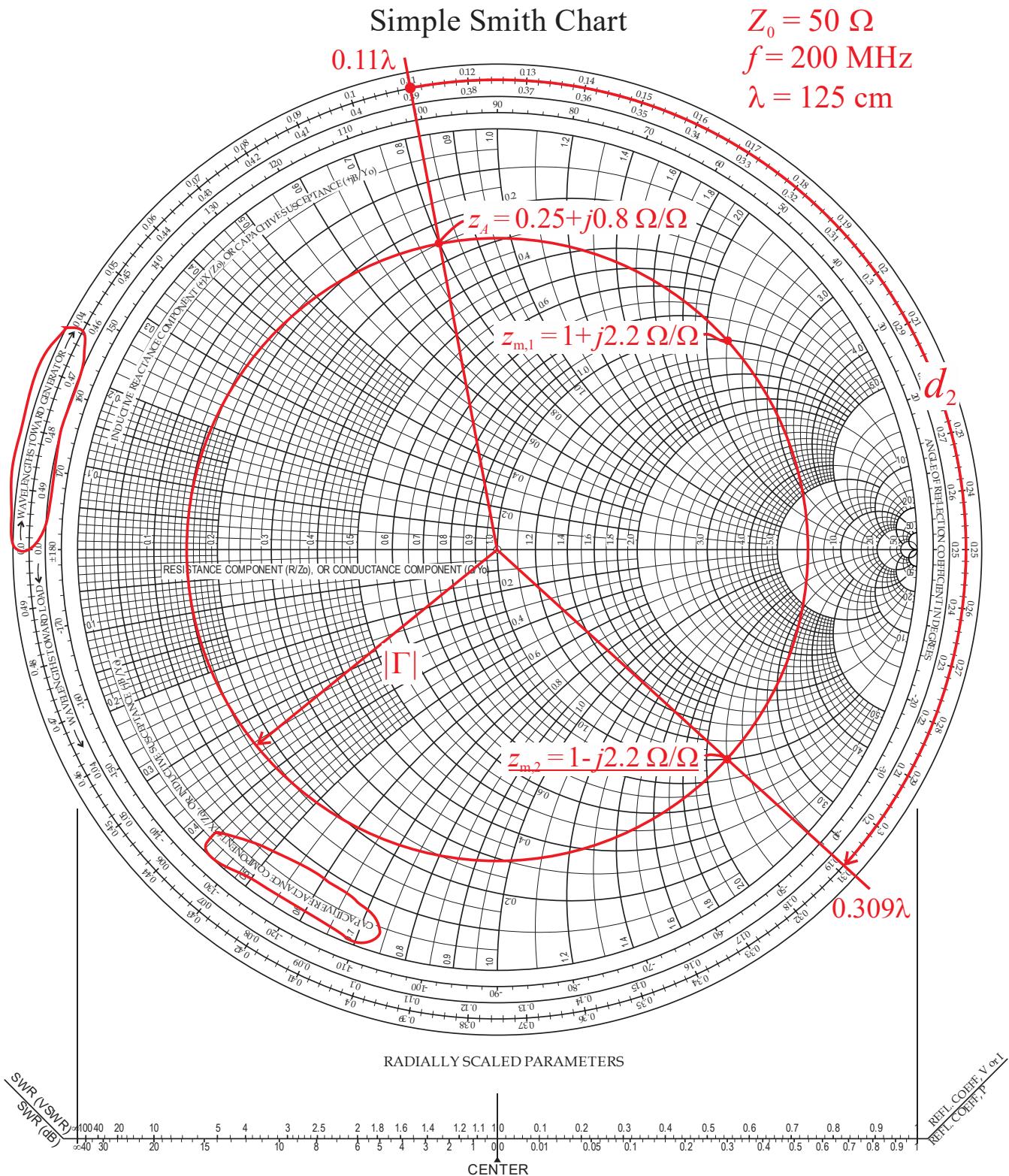
- The wavelength is  $\lambda = c/f = 2.5 \times 10^8/200 \times 10^6 = 1.25 \text{ m} = 125 \text{ cm}$ .

## Steps

- 1) Calculate normalized impedance  $z_A = Z_A/Z_0 = (12.5 + j40)/50 \Rightarrow z_A = 0.25 + j0.8 \Omega/\Omega$  and plot on **Smith chart** (see Figure 2).
- 2) Draw circle, centered on Smith chart, through  $z_A$  point. This circle of constant  $|\Gamma|$  includes the locus of all possible  $z_{in}$  (and  $y_{in}$ ) along the transmission line with this load.
- 3) The two match points are  $z_{m,i} = 1 \pm j2.2 \Omega/\Omega$ . To use a discrete series inductor for matching, select  $z_{m,2} = 1 - j2.2 \Omega/\Omega$  as it has a capacitive reactance. Note, the match point impedance is  $Z_{m,2} = z_{m,2} Z_0 = (1 - j2.2) 50 = 50 - j110 \Omega$ .
- 4) Find the distance  $d_2$  from  $z_A$  to  $z_{m,2}$  using scales on Smith chart,  $d_2 = (0.309 - 0.11) \lambda \Rightarrow d_2 = 0.199\lambda$  or  $d_2 = 0.199(125 \text{ cm}) \Rightarrow d_2 = 24.875 \text{ cm}$ .
- 5) At  $d_2$ , add a discrete inductor in series with reactance  $Z_{ind} = j\omega L = j110 \Omega$ . Solving for  $L$  yields  $L = 110/(2\pi 200 \times 10^6) = 8.7535 \times 10^{-8} \text{ H} \Rightarrow L = 87.535 \text{ nH}$ .
- 6) As shown on Figure 1, everywhere toward the source from the location of  $L$  will be matched, i.e.,  $Z_{in} = 500 \Omega$ .



**Figure 1** Matching antenna using discrete series inductor.



**Figure 2** Smith chart for matching an antenna using discrete series inductor.