

- 5.14** A resonant six-turn loop of *closely spaced turns* is operating at **80 MHz**. The radius of the loop is  $\lambda/30$ , and the loop is connected to a 50-ohm transmission line. The radius of the wire is  $\lambda/300$ , its conductivity is  $\sigma = 5.7 \times 10^7$  S/m, and the spacing between the turns is  $\lambda/100$ . Determine the
- directivity of the antenna (in dB)
  - radiation efficiency taking into account the proximity effects of the turns
  - reflection efficiency
  - gain of the antenna (in dB)
- Note: "resonant" means you assume  $X_A = 0$ . Assume antenna is 'small'.

a)  $C_{\text{single}} = 2\pi a = \frac{2\pi\lambda}{30} = 0.20944\lambda \leftarrow \text{borderline}$   
 For a 'small' antenna, per (5-31)

$$\underline{D_{\text{max}} = D_0 = 3/2 = 10 \log_{10} 3/2 = 1.7609 \text{ dBi}}$$

b) For radiation efficiency, we need  $R_r$  &  $R_L$ .

$$\begin{aligned} \text{From (5-24), } R_{r,1\text{-turn}} &= \eta \left(\frac{\pi}{6}\right) (k^2 a^2) = \eta \left(\frac{\pi}{6}\right) (ka)^4 \\ &= 376.7303 \left(\frac{\pi}{6}\right) \left[\frac{2\pi}{\lambda} \frac{\lambda}{30}\right]^4 \\ &= 0.379545309 \Omega \end{aligned}$$

$$\text{From (5-24a) } R_r = N^2 R_{r,1\text{-turn}} = 6^2 (0.3795453)$$

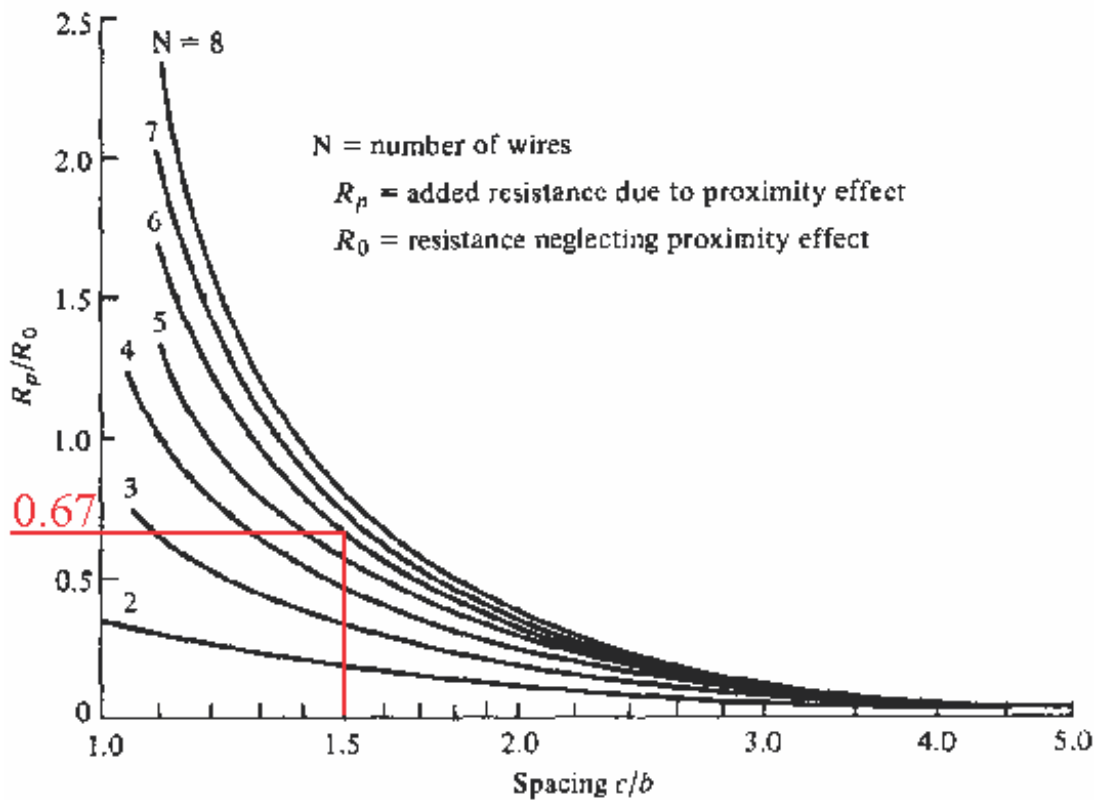
$$\underline{R_r = 13.66363 \Omega}$$

$$\text{From (5-25), } R_L = R_{\text{ohmic}} = \frac{Na}{b} R_s \left(\frac{R_p}{R_0} + 1\right)$$

$$\text{where } R_s = \sqrt{\frac{\omega \mu_0}{2\sigma}}$$

The ratio  $\frac{R_p}{R_0}$  can be found using Fig 5-3 on next page knowing  $N=6$  and

$$\frac{2c}{2b} = \frac{\text{turn spacing}}{\text{wire diameter}} = \frac{\lambda/100}{2 \times \lambda/300} = 1.5 \text{ to be } 0.67.$$



(b) Ohmic resistance due to proximity (after G. N. Smith)

**Figure 5.3**  $N$ -turn circular loop and ohmic resistance due to proximity effect. (SOURCE: G. S. Smith, "Radiation Efficiency of Electrically Small Multiturn Loop Antennas," *IEEE Trans. Antennas Propagat.*, Vol. AP-20, No. 5, pp. 656-657, Sept. 1972<sup>©</sup> (1972) IEEE).

$$b) \text{ cont. } R_L = \frac{6(\frac{1}{30})}{\frac{1}{300}} \sqrt{\frac{2\pi(80 \times 10^6)4\pi \times 10^{-7}}{2(5.7 \times 10^7)}} (0.67 + 1) = \underline{0.23586 \Omega}$$

$$\text{Per (2-90), } e_{cd} = \frac{R_r}{R_r + R_L} = \frac{13.66363}{13.66363 + 0.23586} = \underline{0.983 \text{ or } 98.3\%}$$

$$c) Z_A = R_A + jX_A \xrightarrow{\text{resonant}} R_r + R_L = 13.89949 \Omega$$

$$\Gamma = \frac{Z_A - Z_0}{Z_A + Z_0} = \frac{13.89949 - 50}{13.89949 + 50} = -0.56496$$

$$\text{Per (2-45), } e_r = 1 - |\Gamma|^2 = 1 - (0.56496)^2 = \underline{0.6808 \text{ or } 68.08\%}$$

$$d) \text{ Per (2-49a), } G_0 = e_{cd} D_0 = 0.983 \left(\frac{3}{2}\right) = \underline{1.4745 = 1.686 \text{ dBi}}$$

$$\text{Per (2-49c), the absolute gain } G_{abs} = e_r e_{cd} D_0 = 1.0039 = \underline{0.0169 \text{ dBi}}$$