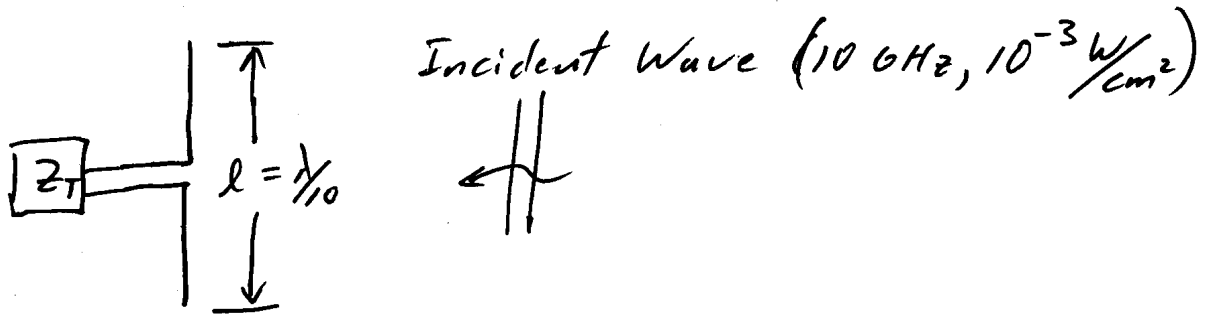


2.72 Repeat Problem 2.71 for a small dipole with triangular current distribution and length $l = \lambda/10$. See Example 2.14.

2.71 A uniform plane wave, of 10^{-3} watts/cm² power density, is incident upon an infinitesimal dipole of length $l = \lambda/50$ and uniform current distribution, as shown in Figure 2.29(a). For a frequency of 10 GHz, determine the maximum open-circuited voltage at the terminals of the antenna. See Problem 2.69.



$$l = \lambda/50 = \frac{1}{50} \frac{2.9979 \times 10^8}{10 \times 10^9} = 0.0029979 \text{ m}$$

From Example 2.14, $\bar{l}_e = -\hat{a}_\theta \frac{l}{2} \sin \theta$ for a small dipole.

$$\text{From notes, } W_{inc} = \frac{|\bar{E}^i|^2}{2\eta} = 10^{-3} \frac{W}{cm^2} \frac{100^2 cm^2}{1^2 m^2}$$

$$|\bar{E}^i| = \sqrt{2\eta W_{inc}} = \sqrt{2(376.7303)10} = 86.80211 \text{ V/m}$$

$$\text{Per (2-93), } V_{oc} = \bar{E}^i \cdot \bar{l}_e$$

For maximum V_{oc} , assume \bar{E}^i in $-\hat{a}_\theta$ direction and arriving at broadside ($\theta = 90^\circ$).

$$V_{oc} = -\hat{a}_\theta 86.80211 \text{ V/m} \cdot -\hat{a}_\theta \frac{0.0029979}{2} \sin 90^\circ$$

$$\underline{V_{oc} = 0.1301 \text{ V}}$$