2.57 The input reactance of an infinitesimal linear dipole of length $\lambda/60$ and radius $a = \lambda/200$ is given by $\lim_{l \to 0} [\ln(l/2a) - 1]$

 $X_{in} \simeq -120 \frac{[\ln(l/2a) - 1]}{\tan(kl/2)}$

Assuming the wire of the dipole is copper with a conductivity of 5.7×10^7 S/m, determine at f = 1 GHz the

- (a) loss resistance
- (b) radiation resistance
- (c) radiation efficiency
- (d) VSWR when the antenna is connected to a 50-ohm line
- with length of $\lambda/50$ and radius of $\lambda/250$. [Hint: look at Chapter 4.]
- a) Since $l = \frac{1}{50}$, we can use the constant current approx. ler(2-906), $R_L = R_{nf} = \frac{l}{P} \sqrt{\frac{\omega \mu_0}{z\sigma}} = \frac{\frac{1}{50}}{2\pi (\frac{1}{250})} \sqrt{\frac{2\pi (1\times 10^9) 4\pi \times 10^{-7}}{2(5.7\times 10^7)}}$
 - $R_L = 0.00662266 R = 6.6227 msl$
- b) Use (4-19) to get radiation resistance $N_r = 80\pi^2 (\frac{1}{\lambda})^2 = 80\pi^2 \left(\frac{\frac{1}{50}}{\lambda}\right)^2 \Rightarrow N_r = 0.31583 \text{ } \text{.}$
- C) Per (2-90), the radiation efficiency is $e_{cd} = \frac{R_r}{R_r + R_L} = \frac{0.31583}{0.31583 + 0.0066} = \frac{0.97946}{0.97946} = \frac{97.95\%}{0.97946}$
- d) X_{In} = -120 ln(\$\frac{1}{2}\frac{1}{250}\) -1 \\ \tan(\frac{27}{7}\frac{1}{50}/2) = 159.6624859 \Lambda

 $Z_{ANT} = R_L + R_r + j X_{in} = 0.31583 + 0.0066227 + j 159.66249 n$ = 0.32245 + j 159.6625 n

 $\int_{ANT} = \frac{2ANT - 20}{2ANT + 20} = \frac{(0.32245 + j.159.66) - 50}{(0.32245 + j.159.66) + 50}$ $= 0.998848735 \left(34.7777^{\circ}\right)$

 $VSWN = \frac{1+1\Gamma_{ANT}I}{1-1\Gamma_{ANT}I} = \frac{1+0.99885}{1-0.99885} \Rightarrow \frac{VSWN = 1736.22}{(essentially ob)}$