

ex. Use a Gamma-Match to drive the
 5 element, channel 43 Yagi-Uda antenna
 (w/out boom), that was previously designed,
 with a 50Ω coaxial transmission line.
 Matching specification $VSWR \leq 1.1$

Yagi-Uda Design Summary

$$f_c = 647 \text{ MHz} \quad \lambda = 46.3 \text{ cm}$$

$$\text{element diameters} = \frac{1}{4}'' = 0.635 \text{ cm} \Rightarrow a = 0.3175 \text{ cm}$$

$$\text{element spacings} = S_{ij} = 0.2\lambda = 9.274 \text{ cm}$$

$$l_1' = 0.48\lambda = 22.24 \text{ cm}$$

$$l_3' = l_5' = 0.419\lambda = 19.41 \text{ cm}$$

$$l_4' = 0.412\lambda = 19.09 \text{ cm}$$

$$l_3 < l_2' < l_1'$$

$$Z_a = 17.35 + j20.59\Omega \quad (\text{No Match})$$

$$G_{\text{in}} = 11.265 \text{ dBi}$$

1st Try

Select Gamma-Match diameter $2a' = \frac{4}{9}'' = a$
 $a' = 0.15875 \text{ cm}$

Gamma-Match spacing $s = 2 \text{ cm}$

Gamma-Match length $l_1' = 5 \text{ cm}$

Driven Element length $l_2' = 0.47d = 21.8 \text{ cm}$

This yields an equivalent radius of $a_e = 0.666 \text{ cm}$
and $Z_0 = 260 \Omega$ (Gamma-Match transmission line),
(see attached MathCad worksheet). Running
a MoM simulation of this Yagi-Uda antenna
with the modified driven element (see
attached NEC sheets) yields:

$$Z_a = 18.36 + j25.39 \Omega \quad \text{Gain} = 11.6 \text{ dB}$$

$$Z_{in} = 27.746 \Omega \quad (w/C = 4.226 \text{ pF})$$

$$VSWR = 1.802 > 1.1$$

\Rightarrow Need to boost real part of
 Z_a to increase Z_{in} + decrease
imaginary part of Z_a (get near
resonance)

Gamma-Match equations

$$\begin{aligned}
 c &:= 2.9979 \cdot 10^8 & f_c &:= 647 \cdot 10^6 & \lambda &:= \frac{c}{f_c} & \lambda &= 0.46335 & k &:= \frac{2 \cdot \pi}{\lambda} & k &= 13.56023 \\
 Z_{\text{desired}} &:= 50 \quad \Omega & d &:= 0.635 \cdot 10^{-2} \text{ m} & a &:= d \cdot 0.5 & a &= 0.003175 \text{ m} \\
 d_{\text{prime}} &:= 0.3175 \cdot 10^{-2} \text{ m} & a_{\text{prime}} &:= d_{\text{prime}} \cdot 0.5 & a_{\text{prime}} &= 0.0015875 \text{ m} & s &:= 2 \cdot 10^{-2} \text{ m} \\
 Z_0 &:= \frac{376.73}{2 \cdot \pi} \cdot \operatorname{acosh} \left[\frac{(s^2 - a^2 - a_{\text{prime}}^2)}{2 \cdot a \cdot a_{\text{prime}}} \right] & Z_0 &= 260.329 \quad \Omega & u &:= \frac{a}{a_{\text{prime}}} & v &:= \frac{s}{a_{\text{prime}}} \\
 & & & & u &= 2 & v &= 12.5984 \\
 \alpha &:= \frac{\operatorname{acosh} \left[\frac{(v^2 - u^2 + 1)}{2 \cdot v} \right]}{\operatorname{acosh} \left[\frac{(v^2 + u^2 - 1)}{2 \cdot v \cdot u} \right]} & \alpha &= 1.36748 & a_e &:= a_{\text{prime}} \cdot e^{\frac{1}{(1+u)^2} \cdot (u^2 \cdot \ln(u) + 2 \cdot u \cdot \ln(v))} \\
 & & & & a_e &= 0.00666 & a_e \cdot 100 &= 0.66609 \text{ cm} \\
 l_{\text{prime}} &:= 10 \cdot 10^{-2} \text{ m} & l_{\text{prime}} \cdot 0.5 &= 0.05 \text{ m} \\
 Z_t &:= j \cdot Z_0 \cdot \tan \left(\frac{k \cdot l_{\text{prime}}}{2} \right) & Z_t &= 209.66289i \quad \Omega & Y_t &:= \frac{1}{Z_t} & Y_t &= -4.77 \cdot 10^{-3} i
 \end{aligned}$$

Za from NEC (a MoM program)

$$\begin{aligned}
 Z_a &:= 18.356 + j \cdot 25.3879 \quad \Omega & Y_a &:= \frac{1}{Z_a} & Y_a &= 0.0187 - 0.02587i \quad \text{Mhos} \\
 Y_{\text{ing}} &:= Y_t + \frac{Y_a \cdot 2}{(1 + \alpha)^2} & Y_{\text{ing}} &= 6.673 \cdot 10^{-3} - 0.014i & \frac{1}{Z_{\text{desired}}} &= 0.02 \quad \text{Mhos} \\
 Z_{\text{ing}} &:= \frac{1}{Y_{\text{ing}}} & Z_{\text{ing}} &= 27.746 + 58.205i \quad \Omega & Z_{\text{desired}} &= 50 \quad \Omega \\
 C &:= \text{if} \left(\operatorname{Im}(Z_{\text{ing}}) > 0, \frac{1}{2 \cdot \pi \cdot f_c \cdot \operatorname{Im}(Z_{\text{ing}})}, 0 \right) & C &= 4.226 \cdot 10^{-12} & C \cdot 10^{12} &= 4.226 \quad \text{pF} \\
 Z_{\text{cap}} &:= \text{if} \left(C > 0, \frac{1}{j \cdot 2 \cdot \pi \cdot f_c \cdot C}, 0 \right) & Z_{\text{cap}} &= -58.205i \quad \Omega \\
 Z_{\text{in}} &:= Z_{\text{cap}} + Z_{\text{ing}} & Z_{\text{in}} &= 27.746 \quad \Omega \\
 \Gamma &:= \frac{(Z_{\text{in}} - Z_{\text{desired}})}{Z_{\text{in}} + Z_{\text{desired}}} & \Gamma &= -0.286 & |\Gamma| &= 0.286 \\
 \text{VSWR} &:= \frac{(1 + |\Gamma|)}{1 - |\Gamma|} & \text{VSWR} &= 1.802
 \end{aligned}$$

1st Try

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CM Yagi-Uda Antenna for UHF channel 43
 CM THIS PROGRAM ASSUMES THAT THERE IS NO BOOM.
 CM
 CM THIS FILE IS USED TO DETERMINE THE INPUT IMPEDANCE OF THE DRIVEN
 CM ELEMENT OF A 5 ELEMENT ANTENNA. CENTER FREQUENCY IS 647 MHz
 CM W/ WAVELENGTH OF 0.46335 m.
 CM
 CM THE DIMENSIONS ARE:
 CM element diameter $d=0.635\text{cm}=0.25\text{in}$, radius $a=d/2=0.3175\text{cm}=0.125\text{in}$,
 CM equivalent radius of Gamma-Match portion of driven element
 CM is $a_e=0.00666\text{ m}$ which has a length of $l'/2=0.05\text{ m} < l_2$
 CM
 CM $l_1=0.48\text{ m}$, $l_2=0.2224\text{m}$, $l_3=15=0.419\text{ m}$, $l_4=0.1941\text{m}$, $l_5=0.412\text{ m}$, $l_6=0.1909\text{m}$,
 CM driven element $l_2=0.47\text{ m}$, $l_7=0.218\text{m}$
 CM ELEMENT SPACINGS $S_{ij}=0.2\text{ m}$, $l_8=0.09267\text{m}$
 CM SELECT SEGMENT LENGTH OF APPROX. $1.25\text{cm}=0.025\text{ m}$
 CM THE DRIVEN SEGMENT IS #9 on 12.
 GW 1 17 -0.1112 0.0 0.0 0.1112 0.0 0.0 0.003175
 GW 2 9 -0.109 0.0 0.09267 0.0 0.0 0.09267 0.003175
 GW 3 4 0.0 0.0 0.09267 0.05 0.0 0.09267 0.00666
 GW 4 5 0.05 0.0 0.09267 0.109 0.0 0.09267 0.003175
 GW 5 15 -0.09705 0.0 0.18534 0.09705 0.0 0.18534 0.003175
 GW 6 15 -0.09545 0.0 0.27801 0.09545 0.0 0.27801 0.003175
 GW 7 15 -0.09705 0.0 0.37068 0.09705 0.0 0.37068 0.003175
 GE 0 0
 FR 0 1 0 0 647 0
 EX 0 3 1 0 1.0 0.0
 RP 0 2 3 0000 0.0 0.0 180.0 90.0
 PT -1
 XQ 0
 EN

11st
 TRY

65

Yagi-Uda Antenna for UHF channel 43 THIS PROGRAM ASSUMES THAT THERE IS NO BOOM.

THIS FILE IS USED TO DETERMINE THE INPUT IMPEDANCE OF THE DRIVEN ELEMENT OF A 5 ELEMENT ANTENNA. CENTER FREQUENCY IS 647 MHZ W/ WAVELENGTH OF 0.46335 m.

THE DIMENSIONS ARE:

element diameter d=0.635cm=0.25in, radius a=d/2=0.3175cm=0.125in,
equivalent radius of Gamma-Match portion of driven element
is ae=0.00666 m which has a length of l'/2=0.05 m < l2

l1=0.48 l=0.2224m, l3=l5=0.419 l=0.1941m, l4=0.412 l=0.1909m,
driven element l2=0.47 l= 0.218m
ELEMENT SPACINGS Sij=0.2 l=0.09267m
SELECT SEGMENT LENGTH OF APPROX. 1.25cm=0.025 l
THE DRIVEN SEGMENT IS #9 on l2.

1st
TRY

- - - STRUCTURE SPECIFICATION - - -

COORDINATES MUST BE INPUT IN METERS OR BE SCALED TO METERS
BEFORE STRUCTURE INPUT IS ENDED

WIRE NO.	NO.	OF	FIRST	LAST	TAG																
	X1	Y1	Z1	X2	Y2	Z2	RADIUS	SEG.	SEG.	SEG.	NO.										
1	-0.11120	0.0	0.0	0.11120	0.0	0.0	0.00317	17	1	17	1										
2	-0.10900	0.0	0.09267	0.0	0.0	0.0	0.09267	0.00317	9	18	26	2									
3	0.0	0.0	0.09267	0.05000	0.0	0.0	0.09267	0.00666	4	27	30	3									
4	0.05000	0.0	0.09267	0.10900	0.0	0.0	0.09267	0.00317	5	31	35	4									
5	-0.09705	0.0	0.18534	0.09705	0.0	0.0	0.18534	0.00317	15	36	50	5									
6	-0.09545	0.0	0.27801	0.09545	0.0	0.0	0.27801	0.00317	15	51	65	6									
7	-0.09705	0.0	0.37068	0.09705	0.0	0.0	0.37068	0.00317	15	66	80	7									

TOTAL SEGMENTS USED= 80 NO. SEG. IN A SYMMETRIC CELL= 80 SYMMETRY FLAG= 0

***** INPUT LINE 1 FR 0 1 0 0 6.47000E+02 0.0 0.0 0.0 0.0 0.0
***** INPUT LINE 2 EX 0 3 1 0 1.00000E+00 0.0 0.0 0.0 0.0 0.0
***** INPUT LINE 3 RP 0 2 3 0 0.0 0.0 1.800E+02 9.000E+01 0.0 0.0

FREQUENCY= 6.4700E+02 MHZ WAVELENGTH= 4.6337E-01 METERS

- - - ANTENNA INPUT PARAMETERS - - -

TAG	SEG.	VOLTAGE	IMPEDANCE (OHMS)	ADMITTANCE (MHOS)	
NO.	NO.	REAL	IMAG.	REAL	IMAG.
3	27	1.0	0.0	1.83560E+01	2.53879E+01

- - - RADIATION PATTERNS - - -

THETA	PHI	Gain
DEGREES	DEGREES	DB
0.00	0.00	11.61220
180.00	0.00	-0.14719

$Z_a = 18.356 + j 25.3879 \Omega$

***** INPUT LINE 4 PT -1 0 0 0 0.0 0.0 0.0 0.0 0.0 0.0
***** INPUT LINE 5 XQ 0 0 0 0 0.0 0.0 0.0 0.0 0.0 0.0
***** INPUT LINE 6 EN 0 0 0 0 0.0 0.0 0.0 0.0 0.0 0.0

2nd Try

→ Decrease l_2' to 20.8 cm

The MoM Simulation (see attached MCAD and NEC sheets) now yields:

$$Z_a = 14.93 + j1.27 \Omega \quad \text{Gain} = 11.56 \text{ dBi}$$

which gives

$$Z_{in} = 38.95 \Omega \quad \text{w/ } C = 22.062 \text{ pF}$$

$$V_{SWR} = 1.284 > 1.1$$

Still need to increase the real part of Z_a . Since the driven element is very close to resonance, further adjustments to l_2' will give minimal return.

Gamma-Match equations

$c := 2.9979 \cdot 10^8$ $fc := 647 \cdot 10^6$ $\lambda := \frac{c}{fc}$ $\lambda = 0.46335$ $k := \frac{2 \cdot \pi}{\lambda}$ $k = 13.56023$

$Z_{desired} := 50 \quad \Omega$ $d := 0.635 \cdot 10^{-2} \text{ m}$ $a := d \cdot 0.5$ $a = 0.003175 \text{ m}$

$d_{prime} := 0.3175 \cdot 10^{-2} \text{ m}$ $a_{prime} := d_{prime} \cdot 0.5$ $a_{prime} = 0.0015875 \text{ m}$ $s := 2 \cdot 10^{-2} \text{ m}$

$Z_0 := \frac{376.73}{2 \cdot \pi} \cdot \text{acosh} \left[\frac{(s^2 - a^2 - a_{prime}^2)}{2 \cdot a \cdot a_{prime}} \right]$ $Z_0 = 260.329 \quad \Omega$ $u := \frac{a}{a_{prime}}$ $v := \frac{s}{a_{prime}}$

$u = 2$ $v = 12.5984$

$\alpha := \frac{\text{acosh} \left[\frac{(v^2 - u^2 + 1)}{2 \cdot v} \right]}{\text{acosh} \left[\frac{(v^2 + u^2 - 1)}{2 \cdot v \cdot u} \right]}$ $\alpha = 1.36748$ $ae := a_{prime} \cdot e^{\frac{1}{(1+u)^2} \cdot (u^2 \cdot \ln(u) + 2 \cdot u \cdot \ln(v))}$

$ae = 0.00666$ $ae \cdot 100 = 0.66609 \text{ cm}$

$l_{prime} := 10 \cdot 10^{-2} \text{ m}$ $l_{prime} \cdot 0.5 = 0.05 \text{ m}$

$Z_t := j \cdot Z_0 \cdot \tan \left(\frac{k \cdot l_{prime}}{2} \right)$ $Z_t = 209.66289i \quad \Omega$ $Y_t := \frac{1}{Z_t}$ $Y_t = -4.77 \cdot 10^{-3} i$

Za from NEC (a MoM program)

$Z_a := 14.9299 + j \cdot 1.27235 \quad \Omega$ $Y_a := \frac{1}{Z_a}$ $Y_a = 0.0665 - 0.00567i$ Mhos

$Y_{ing} := Y_t + \frac{Y_a \cdot 2}{(1 + \alpha)^2}$ $Y_{ing} = 0.024 - 6.792 \cdot 10^{-3} i$ $\frac{1}{Z_{desired}} = 0.02 \text{ Mhos}$

$Z_{ing} := \frac{1}{Y_{ing}}$ $Z_{ing} = 38.953 + 11.15i \quad \Omega$ $Z_{desired} = 50 \quad \Omega$

$C := \text{if} \left(\text{Im}(Z_{ing}) > 0, \frac{1}{2 \cdot \pi \cdot fc \cdot \text{Im}(Z_{ing})}, 0 \right)$ $C = 2.206 \cdot 10^{-11}$ $C \cdot 10^{12} = 22.062 \text{ pF}$

$Z_{cap} := \text{if} \left(C > 0, \frac{1}{j \cdot 2 \cdot \pi \cdot fc \cdot C}, 0 \right)$ $Z_{cap} = -11.15i \quad \Omega$

$Z_{in} := Z_{cap} + Z_{ing}$ $Z_{in} = 38.953 \quad \Omega$

$\Gamma := \frac{(Z_{in} - Z_{desired})}{Z_{in} + Z_{desired}}$ $\Gamma = -0.124$ $|\Gamma| = 0.124$

$VSWR := \frac{(1 + |\Gamma|)}{1 - |\Gamma|}$ $VSWR = 1.284$

2nd Try

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CM Yagi-Uda Antenna for UHF channel 43
CM THIS PROGRAM ASSUMES THAT THERE IS NO BOOM.
CM
CM THIS FILE IS USED TO DETERMINE THE INPUT IMPEDANCE OF THE DRIVEN
CM ELEMENT OF A 5 ELEMENT ANTENNA. CENTER FREQUENCY IS 647 MHz
CM W/ WAVELENGTH OF 0.46335 m.
CM
CM THE DIMENSIONS ARE:
CM element diameter d=0.635cm=0.25in, radius a=d/2=0.3175cm=0.125in,
CM equivalent radius of Gamma-Match portion of driven element
CM is ae=0.00666 m which has a length of l'/2=0.05 m < l2
CM
CM l1=0.48 l=0.2224m, l3=l5=0.419 l=0.1941m, l4=0.412 l=0.1909m,
CM driven element l2=0.4489 l= 0.208m
CM ELEMENT SPACINGS Sij=0.2 l=0.09267m
CM SELECT SEGMENT LENGTH OF APPROX. 1.25cm=0.025 l
CE THE DRIVEN SEGMENT IS #9 on l2.
GW 1 17 -0.1112 0.0 0.0 0.1112 0.0 0.0 0.003175
GW 2 9 -0.104 0.0 0.09267 0.0 0.0 0.09267 0.003175
GW 3 4 0.0 0.0 0.09267 0.05 0.0 0.09267 0.00666
GW 4 5 0.05 0.0 0.09267 0.104 0.0 0.09267 0.003175
GW 5 15 -0.09705 0.0 0.18534 0.09705 0.0 0.18534 0.003175
GW 6 15 -0.09545 0.0 0.27801 0.09545 0.0 0.27801 0.003175
GW 7 15 -0.09705 0.0 0.37068 0.09705 0.0 0.37068 0.003175
GE 0 0
FR 0 1 0 0 647 0
EX 0 3 1 0 1.0 0.0
RP 0 2 3 0000 0.0 0.0 180.0 90.0
PT -1
XQ 0
EN

```

2nd Try

Yagi-Uda Antenna for UHF channel 43 THIS PROGRAM ASSUMES THAT THERE IS NO BOOM.

THIS FILE IS USED TO DETERMINE THE INPUT IMPEDANCE OF THE DRIVEN ELEMENT OF A 5 ELEMENT ANTENNA. CENTER FREQUENCY IS 647 MHZ W/ WAVELENGTH OF 0.46335 m.

THE DIMENSIONS ARE:

element diameter d=0.635cm=0.25in, radius a=d/2=0.3175cm=0.125in, equivalent radius of Gamma-Match portion of driven element is ae=0.00666 m which has a length of l'/2=0.05 m < l2

l1=0.48 l=0.2224m, l3=15=0.419 l=0.1941m, l4=0.412 l=0.1909m, driven element l2=0.4489 l= 0.208m ELEMENT SPACINGS Sij=0.2 l=0.09267m SELECT SEGMENT LENGTH OF APPROX. 1.25cm=0.025 l THE DRIVEN SEGMENT IS #9 on l2.

2nd TRY

- - - STRUCTURE SPECIFICATION - - -

COORDINATES MUST BE INPUT IN METERS OR BE SCALED TO METERS BEFORE STRUCTURE INPUT IS ENDED

WIRE NO.	NO. OF X1	Y1	Z1	LAST X2	Y2	Z2	TAG RADIUS	SEG.	SEG.	SEG.	NO.
1	-0.11120	0.0	0.0	0.11120	0.0	0.0	0.00317	17	1	17	1
2	-0.10400	0.0	0.09267	0.0	0.0	0.0	0.09267	0.00317	9	18	26 2
3	0.0	0.0	0.09267	0.05000	0.0	0.0	0.09267	0.00666	4	27	30 3
4	0.05000	0.0	0.09267	0.10400	0.0	0.0	0.09267	0.00317	5	31	35 4
5	-0.09705	0.0	0.18534	0.09705	0.0	0.0	0.18534	0.00317	15	36	50 5
6	-0.09545	0.0	0.27801	0.09545	0.0	0.0	0.27801	0.00317	15	51	65 6
7	-0.09705	0.0	0.37068	0.09705	0.0	0.0	0.37068	0.00317	15	66	80 7

TOTAL SEGMENTS USED= 80 NO. SEG. IN A SYMMETRIC CELL= 80 SYMMETRY FLAG= 0

***** INPUT LINE 1 FR 0 1 0 0 6.47000E+02 0.0 0.0 0.0 0.0 0.0 ***** INPUT LINE 2 EX 0 3 1 0 1.00000E+00 0.0 0.0 0.0 0.0 0.0 ***** INPUT LINE 3 RP 0 2 3 0 0.0 0.0 1.800E+02 9.00E+01 0.0 0.0

FREQUENCY= 6.4700E+02 MHZ WAVELENGTH= 4.6337E-01 METERS

- - - ANTENNA INPUT PARAMETERS - - -

TAG NO.	SEG. NO.	VOLTAGE REAL	IMAG.	IMPEDANCE REAL	(OHMS) IMAG.	ADMITTANCE REAL	(MHOS) IMAG.
3	27	1.0	0.0	1.49299E+01	1.27235E+00	6.64966E-02	-5.66692E-03

- - - RADIATION PATTERNS - - -

THETA PHI MAJOR DEGREES DEGREES DB 0.00 0.00 11.56149 180.00 0.00 -0.12704

***** INPUT LINE 4 PT -1 0 0 0 0.0 0.0 0.0 0.0 0.0 0.0 ***** INPUT LINE 5 XQ 0 0 0 0 0.0 0.0 0.0 0.0 0.0 0.0 ***** INPUT LINE 6 EN 0 0 0 0 0.0 0.0 0.0 0.0 0.0 0.0

3rd Try

Increase l_1' to 22.4 cm
 & decrease l_3' to 19.1 cm

The MoM simulation (see attached MCAO
 + NEC sheets) now yield:

$$Z_a = 18.2632 - j0.205 \Omega \quad G_{\text{ant}} = 11.46 \text{ dBi}$$

which give

$$Z_{\text{in}} = 48.6 \Omega \quad w/ \quad C = 21.75 \text{ pF}$$

$$\underline{VSWR = 1.03 < 1.1} \quad \text{NONE!}$$

Final Design Summary

$$Z_a = 1/4'' = 0.635 \text{ cm} \quad S_{2j} = 9.274 \text{ cm}$$

$$Z_a' = 1/8'' = 0.3175 \text{ cm}$$

$$S = 2 \text{ cm}$$

$$l_{1/2} = 5 \text{ cm}$$

$$Z_{\text{in}} = 48.6 \Omega$$

$$l_1' = 22.4 \text{ cm}$$

$$C = 21.75 \text{ pF}$$

$$l_2' = 20.8 \text{ cm}$$

$$G_{\text{ant}} = 11.46 \text{ dBi}$$

$$l_3' = 19.1 \text{ cm}$$

$$l_4' = 19.09 \text{ cm}$$

$$l_5' = 19.41 \text{ cm}$$

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Gamma-Match equations

$$c := 2.9979 \cdot 10^8 \quad fc := 647 \cdot 10^6 \quad \lambda := \frac{c}{fc} \quad \lambda = 0.46335 \quad k := \frac{2 \cdot \pi}{\lambda} \quad k = 13.56023$$

$$Z_{desired} := 50 \quad \Omega \quad d := 0.635 \cdot 10^{-2} \text{ m} \quad a := d \cdot 0.5 \quad a = 0.003175 \text{ m}$$

$$d_{prime} := 0.3175 \cdot 10^{-2} \text{ m} \quad a_{prime} := d_{prime} \cdot 0.5 \quad a_{prime} = 0.0015875 \text{ m} \quad s := 2 \cdot 10^{-2} \text{ m}$$

$$Z_0 := \frac{376.73}{2 \cdot \pi} \cdot \text{acosh} \left[\frac{(s^2 - a^2 - a_{prime}^2)}{2 \cdot a \cdot a_{prime}} \right] \quad Z_0 = 260.329 \quad \Omega \quad u := \frac{a}{a_{prime}} \quad v := \frac{s}{a_{prime}}$$

$$u = 2 \quad v = 12.5984$$

$$\alpha := \frac{\text{acosh} \left[\frac{(v^2 - u^2 + 1)}{2 \cdot v} \right]}{\text{acosh} \left[\frac{(v^2 + u^2 - 1)}{2 \cdot v \cdot u} \right]} \quad \alpha = 1.36748$$

$$ae := a_{prime} \cdot e^{\frac{1}{(1+u)^2} \cdot (u^2 \cdot \ln(u) + 2 \cdot u \cdot \ln(v))}$$

$$ae = 0.00666 \quad ae \cdot 100 = 0.66609 \text{ cm}$$

$$l_{prime} := 10 \cdot 10^{-2} \text{ m} \quad l_{prime} \cdot 0.5 = 0.05 \text{ m}$$

$$Z_t := j \cdot Z_0 \cdot \tan \left(\frac{k \cdot l_{prime}}{2} \right) \quad Z_t = 209.66289i \quad \Omega \quad Y_t := \frac{1}{Z_t} \quad Y_t = -4.77 \cdot 10^{-3} i$$

Za from NEC (a MoM program)

$$Z_a := 18.2632 + j \cdot -.205397 \quad \Omega \quad Y_a := \frac{1}{Z_a} \quad Y_a = 0.05475 + 0.00062i \quad \text{Mhos}$$

$$Y_{ing} := Y_t + \frac{Y_a \cdot 2}{(1 + \alpha)^2} \quad Y_{ing} = 0.02 - 4.55 \cdot 10^{-3} i \quad \frac{1}{Z_{desired}} = 0.02 \quad \text{Mhos}$$

$$Z_{ing} := \frac{1}{Y_{ing}} \quad Z_{ing} = 48.555 + 11.309i \quad \Omega \quad Z_{desired} = 50 \quad \Omega$$

$$C := \text{if} \left(\text{Im}(Z_{ing}) > 0, \frac{1}{2 \cdot \pi \cdot fc \cdot \text{Im}(Z_{ing})}, 0 \right) \quad C = 2.175 \cdot 10^{-11} \quad C \cdot 10^{12} = 21.752 \quad \text{pF}$$

$$Z_{cap} := \text{if} \left(C > 0, \frac{1}{j \cdot 2 \cdot \pi \cdot fc \cdot C}, 0 \right) \quad Z_{cap} = -11.309i \quad \Omega$$

$$Z_{in} := Z_{cap} + Z_{ing} \quad Z_{in} = 48.555 \quad \Omega$$

$$\Gamma := \frac{(Z_{in} - Z_{desired})}{Z_{in} + Z_{desired}} \quad \Gamma = -0.015 \quad |\Gamma| = 0.015$$

$$VSWR := \frac{(1 + |\Gamma|)}{1 - |\Gamma|} \quad VSWR = 1.03$$

3rd TRY

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 CM element diameter $d=0.635\text{cm}=0.25\text{in}$, radius $a=d/2=0.3175\text{cm}=0.125\text{in}$,
 CM equivalent radius of Gamma-Match portion of driven element
 CM is $a_e=0.00666\text{ m}$ which has a length of $l'/2=0.05\text{ m} < l_2$
 CM
 CM $l_1=0.483\text{ m}$, $l_3=0.4122\text{ m}$, $l_4=0.412\text{ m}$, $l_5=0.1909\text{m}$,
 CM $l_6=0.419\text{ m}$, $l_7=0.1941\text{m}$
 CM driven element $l_2=0.4489\text{ m}$
 CM ELEMENT SPACINGS $S_{ij}=0.2\text{ m}$
 CM SELECT SEGMENT LENGTH OF APPROX. $1.25\text{cm}=0.025\text{ m}$
 CM THE DRIVEN SEGMENT IS #9 on l_2 .
 GW 1 17 -0.112 0.0 0.0 0.112 0.0 0.0 0.003175
 GW 2 9 -0.104 0.0 0.09267 0.0 0.0 0.09267 0.003175
 GW 3 4 0.0 0.0 0.09267 0.05 0.0 0.09267 0.00666
 GW 4 5 0.05 0.0 0.09267 0.104 0.0 0.09267 0.003175
 GW 5 15 -0.09505 0.0 0.18534 0.09505 0.0 0.18534 0.003175
 GW 6 15 -0.09545 0.0 0.27801 0.09545 0.0 0.27801 0.003175
 GW 7 15 -0.09705 0.0 0.37068 0.09705 0.0 0.37068 0.003175
 GE 0 0
 FR 0 1 0 0 647 0
 EX 0 3 1 0 1.0 0.0
 RP 0 2 3 0000 0.0 0.0 180.0 90.0
 PT -1
 XQ 0
 EN

3rd try

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Yagi-Uda Antenna for UHF channel 43 THIS PROGRAM ASSUMES THAT THERE IS NO BOOM.
THIS FILE IS USED TO DETERMINE THE INPUT IMPEDANCE OF THE DRIVEN
ELEMENT OF A 5 ELEMENT ANTENNA. CENTER FREQUENCY IS 647 MHz
W/ WAVELENGTH OF 0.46335 m.

THE DIMENSIONS ARE:

element diameter d=0.635cm=0.25in, radius a=d/2=0.3175cm=0.125in,
equivalent radius of Gamma-Match portion of driven element
is ae=0.00666 m which has a length of l'/2=0.05 m < l2

l1=0.483 l=0.224m, l3=0.4122 l=0.191 m, l4=0.412 l=0.1909m,
l5=0.419 l=0.1941m
driven element l2=0.4489 l= 0.208m
ELEMENT SPACINGS Sij=0.2 l=0.09267m
SELECT SEGMENT LENGTH OF APPROX. 1.25cm=0.025 l
THE DRIVEN SEGMENT IS #9 on l2.

3rd
TRY

- - - STRUCTURE SPECIFICATION - - -

COORDINATES MUST BE INPUT IN METERS OR BE SCALED TO METERS
BEFORE STRUCTURE INPUT IS ENDED

WIRE NO.	X1	Y1	Z1	LAST X2	Y2	Z2	RADIUS	SEG.	SEG.	SEG.	NO.
1	-0.11200	0.0	0.0	0.11200	0.0	0.0	0.00317	17	1	17	1
2	-0.10400	0.0	0.09267	0.0	0.0	0.0	0.09267	0.00317	9	18	26 2
3	0.0	0.0	0.09267	0.05000	0.0	0.0	0.09267	0.00666	4	27	30 3
4	0.05000	0.0	0.09267	0.10400	0.0	0.0	0.09267	0.00317	5	31	35 4
5	-0.09505	0.0	0.18534	0.09505	0.0	0.0	0.18534	0.00317	15	36	50 5
6	-0.09545	0.0	0.27801	0.09545	0.0	0.0	0.27801	0.00317	15	51	65 6
7	-0.09705	0.0	0.37068	0.09705	0.0	0.0	0.37068	0.00317	15	66	80 7

TOTAL SEGMENTS USED= 80 NO. SEG. IN A SYMMETRIC CELL= 80 SYMMETRY FLAG= 0

***** INPUT LINE 1 FR 0 1 0 0 6.47000E+02 0.0 0.0 0.0 0.0 0.0
 ***** INPUT LINE 2 EX 0 3 1 0 1.00000E+00 0.0 0.0 0.0 0.0 0.0
 ***** INPUT LINE 3 RP 0 2 3 0 0.0 0.0 1.80E+02 9.00E+01 0.0 0.0

FREQUENCY= 6.4700E+02 MHZ WAVELENGTH= 4.6337E-01 METERS

- - - ANTENNA INPUT PARAMETERS - - -

TAG NO.	SEG. NO.	VOLTAGE		IMPEDANCE (OHMS)		ADMITTANCE (MHOS)	
		REAL	IMAG.	REAL	IMAG.	REAL	IMAG.
3	27	1.0	0.0	1.82632E+01	-2.05397E-01	5.47479E-02	6.15721E-04

- - - RADIATION PATTERNS - - -

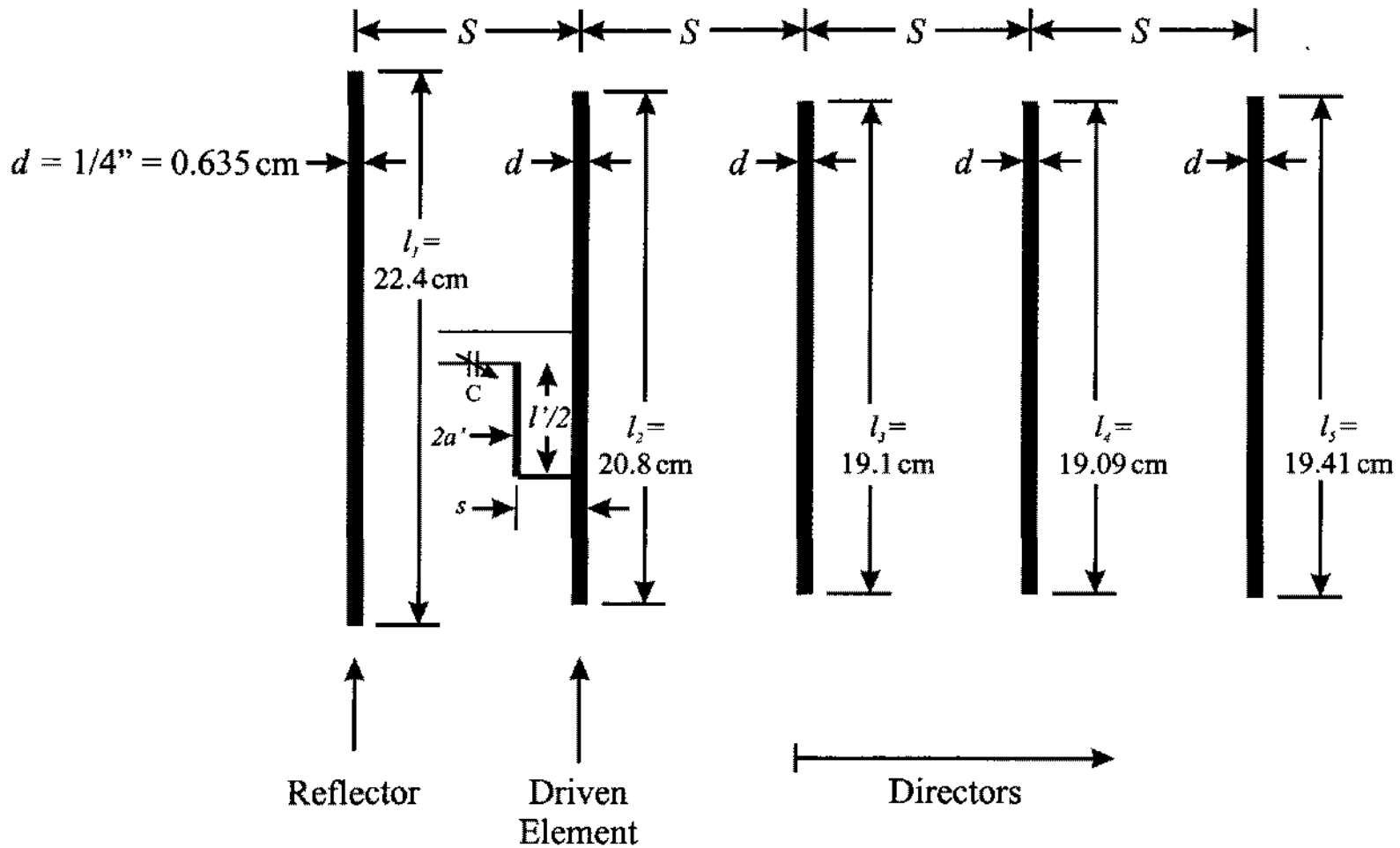
THETA DEGREES	PHI DEGREES	Gain DB
0.00	0.00	11.45567
180.00	0.00	-1.78089

$Z_a = 18.2632 - j 0.205397 \Omega$

***** INPUT LINE 4 PT -1 0 0 0 0.0 0.0 0.0 0.0 0.0 0.0
 ***** INPUT LINE 5 XQ 0 0 0 0 0.0 0.0 0.0 0.0 0.0 0.0
 ***** INPUT LINE 6 EN 0 0 0 0 0.0 0.0 0.0 0.0 0.0 0.0

5 element, channel 43 Yagi-Uda antenna w/ Gamma-Match

$(S = 3.651'' = 9.274 \text{ cm})$



Gamma-Match Dimensions: $2a' = 1/8'' = 0.3175 \text{ cm}$, $s = 2.0 \text{ cm}$, $l'/2 = 5 \text{ cm}$, and $C = 21.75 \text{ pF}$

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