

Design a 75Ω stripline using a ground plane separation of 1.5 mm with an ABS dielectric ($\epsilon_r = 2$, $\tan \delta = 0.005$). Assume the ground planes and land are made with 2 oz. copper (ϵ_0 , μ_0 , $\sigma = 5.7 \times 10^7 \text{ S/m}$). Draw a fully-labeled sketch of the design. At 2 GHz , find: a) the phase velocity, b) guided wavelength, c) phase constant, d) dielectric attenuation constant (Np/m & dB/m), e) conductor attenuation constant (Np/m & dB/m), and f) overall attenuation constant (Np/m & dB/m).

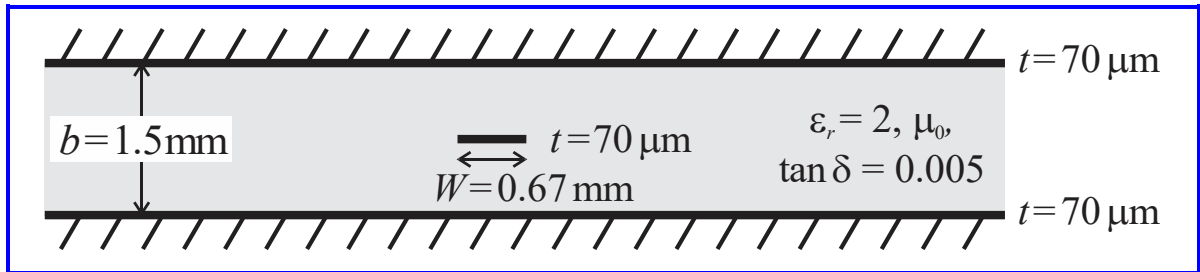
Given dimensions: $b = 1.5 \text{ mm}$ and $t = 70 \mu\text{m}$ (2 oz. copper).

$$\text{Per (3.180a), } \frac{W}{b} = \begin{cases} x & \text{for } \sqrt{\epsilon_r} Z_0 < 120 \Omega \\ 0.85 - \sqrt{0.6 - x} & \text{for } \sqrt{\epsilon_r} Z_0 > 120 \Omega \end{cases} \quad \text{where (3.180b) } x = \frac{30\pi}{\sqrt{\epsilon_r} Z_0} - 0.441.$$

$$\text{Here, } \sqrt{\epsilon_r} Z_0 = \sqrt{2} (75) = 106.066 \Omega < 120 \Omega \text{ and } x = \frac{30\pi}{\sqrt{2} (75)} - 0.441 = 0.447577.$$

Using the bottom equation of (3.180a), $\frac{W}{b} = x = 0.447577$. Therefore, the land width is

$$W = x b = (0.447577)1.5 \Rightarrow \underline{W = 0.6714 \text{ mm.}}$$



$$\text{a) Per (3.76), } v_p = \frac{c}{\sqrt{\epsilon_r}} = \frac{2.9979 \times 10^8}{\sqrt{2}} \Rightarrow \underline{v_p = 2.11985 \times 10^8 \text{ m/s.}}$$

$$\text{b) } \lambda_g = \frac{v_p}{f} = \frac{2.11985 \times 10^8}{2 \times 10^9} \Rightarrow \underline{\lambda_g = 0.10599 \text{ m} = 10.6 \text{ cm.}}$$

$$\text{c) Per (3.177), } \beta = \frac{\omega}{v_p} = \frac{2\pi(2 \times 10^9)}{2.11985 \times 10^8} \Rightarrow \underline{\beta = 59.27945 \text{ rad/m.}}$$

[Note: For a TEM wave, $k = \beta$.]

d) Per (3.30), $\alpha_d = \frac{k \tan \delta}{2} = \frac{59.27945(0.005)}{2} \Rightarrow \underline{\alpha_d = 0.1482 \text{ Np/m} = 1.2872 \text{ dB/m.}}$

e) Per (3.181), $\alpha_c = \begin{cases} \frac{2.7 \times 10^{-3} R_s \epsilon_r Z_0}{30\pi(b-t)} A & \text{for } \sqrt{\epsilon_r} Z_0 < 120 \Omega \\ \frac{0.16 R_s}{Z_0 b} B & \text{for } \sqrt{\epsilon_r} Z_0 > 120 \Omega \end{cases}$

where $A = 1 + \frac{2W}{b-t} + \frac{1}{\pi} \frac{b+t}{b-t} \ln\left(\frac{2b-t}{t}\right)$ and

$B = 1 + \frac{b}{0.5W + 0.7t} \left[0.5 + \frac{0.414t}{W} + \frac{1}{2\pi} \ln\left(\frac{4\pi W}{t}\right) \right]$. Here, $\sqrt{\epsilon_r} Z_0 = 106.066 \Omega$.

Per (1.125), $R_s = \sqrt{\frac{\omega \mu}{2\sigma}} = \sqrt{\frac{2\pi(2 \times 10^9)4\pi \times 10^{-7}}{(2)5.7 \times 10^7}} \Rightarrow R_s = 0.011769 \Omega$

$A = 1 + \frac{2(0.6714 \times 10^{-3})}{1.5 \times 10^{-3} - 70 \times 10^{-6}} + \frac{1}{\pi} \left(\frac{1.5 \times 10^{-3} + 70 \times 10^{-6}}{1.5 \times 10^{-3} - 70 \times 10^{-6}} \right) \ln\left(\frac{2(1.5 \times 10^{-3}) - 70 \times 10^{-6}}{70 \times 10^{-6}}\right)$
 $\Rightarrow A = 3.244.$

$\alpha_c = \frac{2.7 \times 10^{-3} (0.01177) 2(75)}{30\pi(1.5 \times 10^{-3} - 70 \times 10^{-6})} (3.244) \Rightarrow \underline{\alpha_c = 0.1147 \text{ Np/m} = 1.2872 \text{ dB/m.}}$

f) The overall attenuation constant at 2 GHz is

$\alpha_d + \alpha_c = 0.1482 + 0.1147 \Rightarrow \underline{\alpha = 0.2629 \text{ Np/m} = 2.2838 \text{ dB/m.}}$