

3.19 A copper stripline transmission line is to be designed for a $100\ \Omega$ characteristic impedance. The ground plane separation is 1.02 mm and the dielectric constant is 2.20 , with $\tan\delta = 0.001$. At 5 GHz , find the guide wavelength on the line and the total attenuation.

- Assume the land is 1 oz. copper. Draw a fully-labeled sketch of the design.

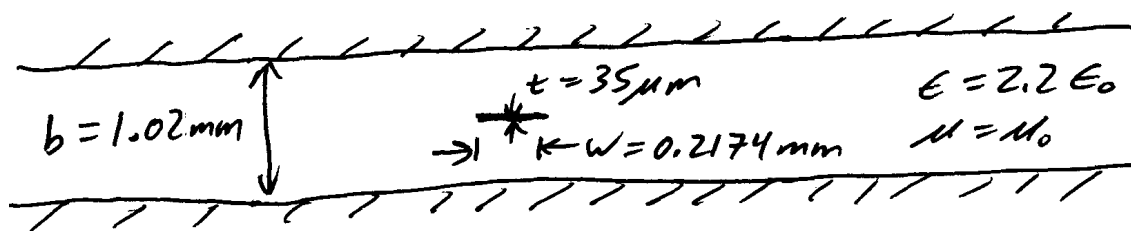
The parameter $\sqrt{\epsilon_r} Z_0 = \sqrt{2.2} 100 = 148.3\ \Omega$ is needed for (3.180a & b) and (3.181).

$$(3.180b) \quad x = \frac{30\pi}{\sqrt{\epsilon_r} Z_0} - 0.441 = \frac{30\pi}{148.3} - 0.441 = 0.194418$$

Use bottom equation of (3.180a)

$$\frac{w}{b} = 0.85 - \sqrt{0.6 - x} = 0.213147$$

$$w = 0.213147(1.02\text{ mm}) = \underline{\underline{0.21741\text{ mm}}}$$



$$\text{Per (3.176), } v_p = \frac{c}{\sqrt{\epsilon_r}} = \frac{2.9979 \times 10^8}{\sqrt{2.2}} = 2.0212 \times 10^8 \text{ m/s}$$

$$\lambda_g = \frac{v_p}{f} = \frac{2.0212 \times 10^8}{5 \times 10^9}$$

$$\lambda_g = \underline{\underline{0.040424\text{ m} = 4.0424\text{ cm}}}$$

Find dielectric attenuation constant using (3.30)

$$\alpha_d = \frac{k \tan \delta}{2} = \frac{2\pi(5 \times 10^9) \sqrt{4\pi \times 10^{-7}} (2.2) 8.854 \times 10^{-12} 0.001}{2}$$

$$\alpha_d = 0.07772 \text{ Np/m}$$

Find conduction attenuation constant from bottom equation $\sqrt{\epsilon_r} z_0 > 120 \Omega$ of (3.181)

$$\alpha_c = \frac{0.16 R_s}{z_0 b} \beta$$

$$\text{where } (1.125) R_s = \sqrt{\frac{\omega \mu}{2\sigma}} = \sqrt{\frac{2\pi(5 \times 10^9) 4\pi \times 10^{-7}}{2(5.813 \times 10^7)}}$$

$$= 0.018427 \Omega$$

→ Copper is non-magnetic (μ_0) and $\sigma_{cu} = 5.813 \times 10^7 \text{ S/m}$
from Appendix F of text

$$\text{From text, } \beta = 1 + \frac{b}{0.5W + 0.7t} \left[0.5 + \frac{0.414t}{W} + \frac{1}{2\pi} \ln \left(\frac{4\pi W}{t} \right) \right]$$

$$\beta = 1 + \frac{1.02 \times 10^{-3}}{0.5(2.1741 \times 10^{-4}) + 0.7(35 \times 10^{-6})} \left[0.5 + \frac{0.414(35 \times 10^{-6})}{2.1741 \times 10^{-4}} + \frac{1}{2\pi} \ln \left(\frac{4\pi 2.174 \times 10^{-4}}{35 \times 10^{-6}} \right) \right]$$

$$= 1 + 7.6574 [0.5 + 0.06665 + 0.69351] = 10.64951$$

$$\alpha_c = \frac{0.16(0.018427)}{100(1.02 \times 10^{-3})} 10.64951 \Rightarrow \alpha_c = 0.30783 \text{ Np/m}$$

$$\alpha = \alpha_c + \alpha_d = 0.30783 + 0.07772 \Rightarrow \boxed{\alpha = 0.38555 \text{ Np/m}}$$

$$\boxed{\alpha = 3.349 \text{ dB/m}}$$