

For the parallel plate transmission line in 1), calculate: a) propagation constant, b) attenuation constant (both Np/m and dB/m), c) phase constant, d) characteristic impedance (both polar & rectangular forms), e) wavelength, and f) phase velocity.

$$\text{From 1), } f = 3 \text{ GHz, } R = 1.73397 \, \Omega/\text{m}$$

$$L = 785.4 \, \text{nH}/\text{m}$$

$$C = 14.592 \, \text{pF}/\text{m}$$

$$G = 27.505 \, \mu\text{S}/\text{m}$$

$$\text{a) Per (2.5), } \gamma = \sqrt{(R + j\omega L)(G + j\omega C)}$$

$$= \sqrt{(1.734 + j2\pi(3 \times 10^9)(7.854 \times 10^{-7}))(2.75 \times 10^{-5} + j2\pi(3 \times 10^9)(1.46 \times 10^{-11}))}$$

$$\gamma = 0.00693 + j63.8115 \, \text{m}^{-1}$$

$$\text{b) Per (2.5), } \alpha = \text{Re}(\gamma) = 0.00693 \, \text{Np}/\text{m} = 6.92755 \times 10^{-3} \, \text{Np}/\text{m}$$

$$\text{OR } \alpha \left(\frac{20 \log e \, \text{dB}}{1 \, \text{Np}} \right) = 0.06017 \, \text{dB}/\text{m}$$

$$\text{c) Per (2.5), } \beta = \text{Im}(\gamma) = 63.8115 \, \text{rad}/\text{m}$$

$$\text{d) Per (2.7), } Z_0 = \sqrt{\frac{R + j\omega L}{G + j\omega C}} = 232.00213 - j0.0019866 \, \Omega$$

$$= 232.002 \angle -0.00049^\circ \, \Omega$$

$$\text{e) Per (2.10), } \lambda = \frac{2\pi}{\beta} = \frac{2\pi}{63.8115} \Rightarrow \lambda = 0.098465 \, \text{m} = 9.85 \, \text{cm}$$

$$\text{f) Per (2.11), } v_p = \frac{\omega}{\beta} = \frac{2\pi(3 \times 10^9)}{63.8115} = 2.95394 \times 10^8 \, \text{m}/\text{s}$$