

Use information from problem 2) to find the **exact**: a) input power, b) load power, c) power lost in TL, d) power from generator, and e) power consumed by Z_g .

Use a 1 m length of the coaxial transmission line from 1) to create a TL circuit with $V_g = 16\angle 0^\circ$ V, $Z_g = 45 - j10 \Omega$, and $Z_L = 100 - j50 \Omega$ operating at 3.6 GHz. Find: a) the load reflection coefficient, b) input reflection coefficient, c) V_0^+ , d) general phasor voltage & current equations.

From earlier problem- $Z_{in} = 90.8596 - j5.8269 \Omega$, $\Gamma_L = 0.4691\angle -24.6237^\circ$,

$$\Gamma_{in} = 0.3202\angle -5.2318^\circ, \quad V_0^+ = 6.6702\angle 13.9394^\circ \text{ V. For } -1 \text{ m} \leq z \leq 0,$$

$$V(z) = (6.67\angle 13.94^\circ) \left[e^{-(0.191+j119.2)z} + (0.469\angle -24.62^\circ) e^{(0.191+j119.2)z} \right] \text{ (V)}$$

$$I(z) = (0.14175\angle 13.89^\circ) \left[e^{-(0.191+j119.2)z} - (0.469\angle -24.624^\circ) e^{(0.191+j119.2)z} \right] \text{ (A)}$$

A coaxial transmission line, operating at 3.6 GHz, has the distributed parameters $R = 3.8 \Omega/\text{m}$, $L = 248 \text{ nH}/\text{m}$, $G = 6.4 \text{ mS}/\text{m}$, and $C = 112 \text{ pF}/\text{m}$. <snip>

From earlier problem-

$$\gamma = 0.19096 + j119.2113 \text{ 1/m}, \quad Z_0 = 47.0561 + j0.435 \Omega = 47.0561\angle 0.05297^\circ \Omega,$$

a) Input power

$$V_{in} = V(-1\text{m}) = (6.67\angle 13.94^\circ) \left[e^{(0.191+j119.2)} + (0.469\angle -24.62^\circ) e^{-(0.191+j119.2)} \right]$$

$$= 10.6504\angle 2.9753^\circ \text{ (V)}$$

$$I_{in} = I(-1\text{m}) = (0.14175\angle 13.89^\circ) \left[e^{(0.191+j119.2)} - (0.469\angle -24.624^\circ) e^{-(0.191+j119.2)} \right]$$

$$= 0.11698\angle 6.6447^\circ \text{ (A)}$$

$$\text{Per (2.92), } P_{in} = 0.5 \text{ Re}\{V_{in} I_{in}^*\} = 0.5 \text{ Re}\{(10.65\angle 2.975^\circ)(0.117\angle -6.645^\circ)\}$$

$$\Rightarrow \underline{P_{in} = 0.62165 \text{ W.}}$$

b) Load power

$$V_L = V(0) = (6.67\angle 13.94^\circ) [1 + (0.469\angle -24.62^\circ)] = 9.6033\angle 6.137^\circ \text{ (V)}$$

$$I_L = I(0) = V_L / Z_L = (9.6033\angle 6.137^\circ) / (100 - j50) = 0.08589\angle 32.703^\circ \text{ (A)}$$

$$\text{Per (2.93), } P_L = 0.5 \text{ Re}\{V(0) I(0)^*\} = 0.5 \text{ Re}\{(9.6033\angle 6.137^\circ)(0.08589\angle -32.703^\circ)\}$$

$$\Rightarrow \underline{P_L = 0.3689 \text{ W.}}$$

c) Power lost in TL

$$\text{Per (2.94), } P_{loss} = P_{in} - P_L = 0.62165 - 0.3689$$

$$\Rightarrow \underline{P_{loss} = 0.25275 \text{ W.}}$$

d) Power from generator

Per circuit theory, $P_{\text{gen}} = 0.5 \operatorname{Re}\{V_g I_{\text{in}}^*\} = 0.5 \operatorname{Re}\{(16\angle 0^\circ)(0.117\angle -6.645^\circ)\}$

$$\Rightarrow \underline{P_{\text{gen}} = 0.92953 \text{ W.}}$$

e) power consumed by Z_g

Per circuit theory, $P_{Zg} = 0.5 |I_{\text{in}}|^2 R_g = 0.5 (0.117)^2 45$

$$\Rightarrow \underline{P_{Zg} = 0.30788 \text{ W.}}$$

As a check, ensure conservation of power holds true-

$$P_{\text{gen}} = P_{Zg} + P_{\text{in}} ?$$

$$0.92953 \text{ W} = 0.30788 + 0.62165 = 0.92953 \text{ W} \therefore$$