

A Victorian brass and beeswax coaxial transmission line operates at 2.5 GHz has the distributed parameters $R = 4 \Omega/\text{m}$, $L = 264 \text{ nH}/\text{m}$, $G = 4.1 \text{ mS}/\text{m}$, and $C = 105 \text{ pF}/\text{m}$. Calculate the a) propagation constant, b) attenuation constant (both Np/m and dB/m), c) phase constant, d) characteristic impedance (both polar & rectangular forms), e) wavelength, and f) phase velocity (m/s and fraction of c).

$$\begin{aligned} \text{a) (2.5)} \quad \gamma &= \sqrt{(R + j\omega L)(G + j\omega C)} = \alpha + j\beta \\ &= \sqrt{(4 + j2\pi(2.5 \times 10^9)(264 \times 10^{-9}))(4.1 \times 10^{-3} + j2\pi(2.5 \times 10^9)(105 \times 10^{-12}))} \\ \gamma &= 0.1427 + j82.7021 \text{ } \underline{\underline{\text{Np}/\text{m}}} \end{aligned}$$

$$\text{b) } \underline{\underline{\alpha = 0.1427 \text{ Np}/\text{m}}} \text{ OR } \alpha = 0.1427(20 \log e) = \underline{\underline{1.239 \text{ dB}/\text{m}}}$$

$$\text{c) } \underline{\underline{\beta = \text{Im}(\gamma) = 82.7021 \text{ rad}/\text{m}}}$$

$$\begin{aligned} \text{d) (2.7)} \quad Z_0 &= \sqrt{\frac{R + j\omega L}{G + j\omega C}} = \sqrt{\frac{4 + j2\pi(2.5 \times 10^9)(264 \times 10^{-9})}{4.1 \times 10^{-3} + j2\pi(2.5 \times 10^9)(105 \times 10^{-12})}} \\ Z_0 &= 50.1426 + j0.0381 \Omega = 50.1426 \angle 0.0436^\circ \Omega \end{aligned}$$

$$\begin{aligned} \text{e) (2.10)} \quad \lambda &= \frac{2\pi}{\beta} = \frac{2\pi}{82.702} \Rightarrow \lambda = 0.075974 \text{ m} \\ &= \underline{\underline{7.5974 \text{ cm}}} \end{aligned}$$

$$\begin{aligned} \text{f) (2.11)} \quad v_p &= \frac{\omega}{\beta} = f\lambda = 2.5 \times 10^9 (7.5974 \times 10^{-2}) \\ v_p &= \underline{\underline{1.89934 \times 10^8 \text{ m/s}}} \end{aligned}$$

$$\frac{v_p}{c} \times 100\% = \frac{1.89934 \times 10^8}{2.9979 \times 10^8} \times 100\% = \underline{\underline{63.355\%}}$$

$$\text{OR } \underline{\underline{v_p = 0.634c}}$$