

**2.23** A slotted-line experiment is performed with the following results: distance between successive minima = 2.1 cm; distance of first voltage minimum from load = 0.9 cm; SWR of load = 3. If  $Z_0 = 50 \Omega$ , find the load impedance.

- Using 'SWR (VSWR)' at below Smith chart on left, set compass to  $\text{SWR} = 3$ .
- Draw a circle, centered on the Smith chart. This circle represents all possible impedances on the transmission line.
- As everything repeats every  $\lambda/2$  on a Smith chart, the distance between voltage minima =  $\lambda/2 = 2.1 \text{ cm} \Rightarrow \lambda = 4.2 \text{ cm}$ .
- Voltage minima occur at  $r_{\min}$ , i.e., where the circle intersects the real axis to the left of center. Mark this location on Smith chart.
- The distance from the closest voltage minima to the load in terms of wavelengths is  $\ell_{\min} / \lambda = 0.9 / 4.2 \Rightarrow \ell_{\min} / \lambda = 0.2143$ .
- Draw radial line from center of Smith chart to 0.2143 on the 'WAVELENGTHS TOWARD LOAD' scale.
- Move  $\ell_{\min} / \lambda = 0.2143$  in the 'WAVELENGTHS TOWARD LOAD' direction from the  $r_{\min}$  point to the location of  $z_L$  on the circle of constant SWR = 3.
- Read-off the normalized load resistance  $r_L = 2.15$  and reactance  $x_L = -1.25$ . This yields  $z_L = 2.15 - j 1.25 \Omega/\Omega$ .
- Find load impedance by multiplying  $z_L$  with  $Z_0$  to get
 
$$Z_L = Z_0 z_L = 50 (2.15 - j 1.25) \Rightarrow \underline{Z_L = 107.5 - j 62.5 \Omega}.$$

2.23 mod 1

Simple  
Smith Chart

$$Z_0 = 50 \Omega$$

$$\lambda = 4.2 \text{ cm}$$

