

A 3 GHz plane wave propagates through nylon (610) in the -z-direction. a) Find the phase velocity, wavelength, attenuation constant, phase constant, and intrinsic impedance. b) If the electric field has an amplitude of 9 V/m at  $z = 0$  and is oriented in the x-direction, write the equation for the phasor vector electric field. c) Find the corresponding phasor vector magnetic field. d) Is nylon (610) a good conductor? Why or why not? Regardless, find the skin depth in nylon (610) at 3 GHz.

From App. G & earlier problem,  $\epsilon_r = 2.84$  &  $\tan \delta = 0.012$  for nylon (610) at 3 GHz. So,  $\epsilon' = 2.84 \epsilon_0 = 2.5146 \times 10^{-11}$  F/m,  $\epsilon'' = \epsilon' \tan \delta = 3.0175 \times 10^{-13}$  F/m, &  $\sigma = \epsilon'' \omega = 5.6879 \times 10^{-3}$  S/m.

a) Use equations from Table 1.1 for general lossy medium

$$\begin{aligned} \text{propagation constant } \gamma &= j\omega\sqrt{\mu\epsilon'}\sqrt{1 - j\frac{\sigma}{\omega\epsilon'}} = j\omega\sqrt{\mu\epsilon'}\sqrt{1 - j\tan\delta} \\ &= j2\pi 3 \cdot 10^9 \sqrt{4\pi \cdot 10^{-7} (2.5146 \cdot 10^{-11})} \sqrt{1 - j0.012} \\ &\Rightarrow \gamma = 0.635745 + j105.96133 \text{ 1/m} = \alpha + j\beta \end{aligned}$$

$$\text{Phase velocity } v_p = \omega / \beta = 2\pi(3 \cdot 10^9) / 105.96133 \Rightarrow \underline{v_p = 1.77891 \times 10^8 \text{ m/s}}$$

$$\text{Wavelength } \lambda = 2\pi / \beta = 2\pi / 105.96133 \Rightarrow \underline{\lambda = 0.059297 \text{ m}}$$

$$\text{attenuation constant } \alpha = \text{Re}(\gamma) = \text{Re}(0.635745 + j105.96133) \Rightarrow \underline{\alpha = 0.635745 \text{ Np/m}}$$

$$\text{phase constant } \beta = \text{Im}(\gamma) = \text{Im}(0.635745 + j105.96133) \Rightarrow \underline{\beta = 105.96133 \text{ rad/m}}$$

$$\text{intrinsic impedance } \eta = \frac{j\omega\mu}{\gamma} = \frac{j(2\pi 3 \cdot 10^9)4\pi \cdot 10^{-7}}{0.635745 + j105.96133} \Rightarrow \underline{\eta = 223.5362 + j1.3412 \Omega}$$

b) Per (1.54),  $E_x(z) = E^+ e^{-\gamma z} + E^- e^{\gamma z}$ . For a wave that propagates in the -z-direction, we drop the first term. Given that  $E_x(z=0) = 9 \text{ V/m} = E^- e^0$ , we get  $E^- = 9 \text{ V/m}$ . Adding the unit vector and  $\gamma$  yields-

$$\Rightarrow \underline{\bar{E} = \hat{x} 9 e^{0.6357z} e^{j105.9613z} \text{ (V/m)}}$$

c) Using (1.58) for a wave that propagates in the -z-direction and adding the unit vector,

$$\begin{aligned} \bar{H} &= -\hat{y} \frac{1}{\eta} E^- e^{\gamma z} = -\hat{y} \frac{1}{223.5362 + j1.3412} 9 e^{0.6357z} e^{j105.9613z} \\ &\Rightarrow \underline{\bar{H} = -\hat{y} (0.0402605 - j0.00024155) e^{0.6357z} e^{j105.9613z} \text{ (A/m)}} \\ &\quad \underline{= -\hat{y} (0.00261 \angle -0.34376^\circ) e^{0.6357z} e^{j105.9613z} \text{ (A/m)}} \end{aligned}$$

d) Check if  $\sigma \gg \epsilon\omega$ , i.e.,  $\tan \delta \gg 1$ ? Since  $\tan \delta = 0.012$ ,

$$\Rightarrow \underline{\text{Nylon (610) is NOT a good conductor.}}$$

$$\text{Per (1.60), the skin depth is } \delta_s = 1/\alpha = 1/0.635745 \Rightarrow \underline{\delta_s = 1.57296 \text{ m}}$$