



For the lossless transmission line circuit shown: $f = 500$ MHz, $v_p = 2 \times 10^8$ m/s, $l = 1.242$ m, $Z_0 = 75 \Omega$, and $\Gamma_{in} = 0.8 \angle -117.5^\circ$.

1) Plot input reflection coefficient and find VSWR

- Use straight edge to draw radial line from center of Smith chart through the -117.5° mark on the “ANGLE OF REFLECTION COEFFICIENT IN DEGREES” scale.
- Use “REFL. COEFF. V or I” scale at bottom right to set compass to $|\Gamma| = 0.8$, and draw arc, centered on Smith chart, through -117.5° radial line.
- The intersection of radial line & arc marks $\Gamma_{in} = 0.8 \angle -117.5^\circ$.
- Use compass to draw $|\Gamma| = 0.8$ arc, centered on Smith chart scales, through SWR (VSWR) scale on bottom left. Read **VSWR = 9**.

2) Find input impedance

- At $\Gamma_{in} = 0.8 \angle -117.5^\circ$ point, locate and read/interpolate value of appropriate “ r ” circle as $r_{in} = 0.15$.
- At $\Gamma_{in} = 0.8 \angle -117.5^\circ$ point, locate and read/interpolate value of appropriate “ x ” arc as $x_{in} = -0.60$.
- Put together to get normalized input impedance $z_{in} = 0.15 - j0.60 \Omega/\Omega$.
- Find input impedance by multiplying z_{in} w/ characteristic impedance to get $Z_{in} = Z_0 z_{in} = 75(0.15 - j0.60) \Rightarrow \underline{\underline{Z_{in} = 11.25 - j45 \Omega}}$.

3) Find load reflection coefficient

- Calculate $l/\lambda = lf/v_p = 1.242(500 \times 10^6)/2 \times 10^8 = 3.105$. Subtract $6(0.5) = 3$ (i.e., remove integer multiples of $n\lambda/2$) to get $\Rightarrow \underline{l/\lambda = 0.105}$.
- Leave compass set to $|\Gamma| = 0.8$ and draw circle centered on Smith chart.
- Using radial line for $\angle\Gamma_{in} = -117.5^\circ$, read 0.087 on the “WAVELENGTHS TOWARD LOAD” scale. Add $0.087 + l/\lambda$ to get 0.192 and draw a radial line from the center of the Smith chart through this point on the scale.
- Use “ANGLE OF REFLECTION COEFFICIENT IN DEGREES” scale to read $\underline{\angle\Gamma_L = -41.6^\circ}$.
- Put magnitude and angle together to get $\underline{\Gamma_L = 0.8\angle-41.6^\circ}$.

4) Find load impedance

- At $\Gamma_L = 0.8\angle-41.6^\circ$ point, locate and read/interpolate value of appropriate “r” circle as $\underline{r_L = 0.8}$.
- At $\Gamma_L = 0.8\angle-41.6^\circ$ point, locate and read/interpolate value of appropriate “x” arc as $\underline{x_L = -2.4}$.
- Put together to get normalized load impedance $\underline{z_L = 0.8 - j2.4 \Omega/\Omega}$.
- Find load impedance by multiplying z_L w/ characteristic impedance to get $Z_L = Z_0 z_L = 75(0.8 - j2.4) \Rightarrow \underline{Z_L = 60 - j180 \Omega}$.

Simple
Smith Chart

$\lambda = 1.242 \text{ m}$

$Z_0 = 75 \Omega$

$V_p = 2 \times 10^8 \text{ m/s}$

