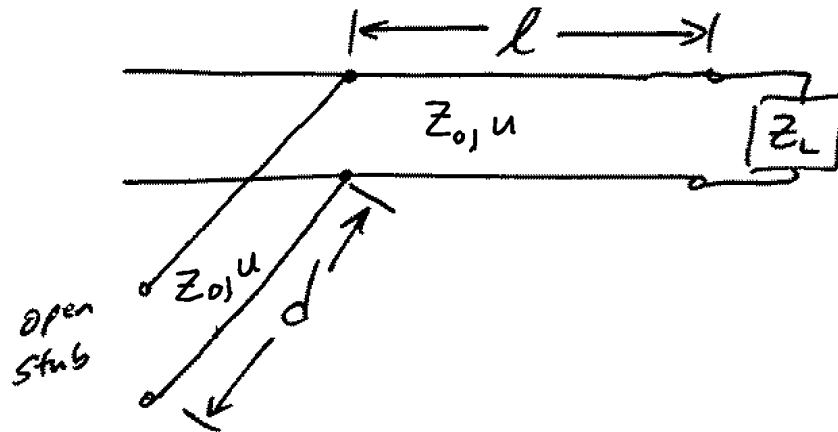


PE 11.7 A 75Ω lossless line is to be matched to a load of $100 - j80 \Omega$ with an **open circuit** stub. Calculate the stub length, its distance from the load, and the necessary stub admittance.

- Find both possible solutions, and sketch resulting circuits.



$$1) \quad \begin{aligned} \gamma_L &= \frac{Z_L}{Z_0} = \frac{100 - j80}{75} = 1.3 - j1.06 \text{ } \Omega/Z \\ \gamma_L &= \frac{1}{\gamma_L} = 0.4573 + j0.36585 \text{ } S/S \end{aligned} \quad \left. \vphantom{\begin{aligned} \gamma_L &= \frac{Z_L}{Z_0} = \frac{100 - j80}{75} = 1.3 - j1.06 \text{ } \Omega/Z \\ \gamma_L &= \frac{1}{\gamma_L} = 0.4573 + j0.36585 \text{ } S/S \end{aligned}} \right\} \text{plot on Smith Chart}$$

2) Draw circle through γ_L & γ_L

3) Note two match points & distances from γ_L

$$\gamma_{m1} = 1 + j0.97 \text{ } S/S, \quad l_1 = 0.1615\lambda - 0.067\lambda = \underline{\underline{0.0945\lambda}}$$

$$\gamma_{m2} = 1 - j0.97 \text{ } S/S, \quad l_2 = 0.339\lambda - 0.067\lambda = \underline{\underline{0.272\lambda}}$$

4) Find lengths of open circuit stubs so that

$$\gamma_{\text{stub1}} = -j0.97 \text{ } S/S \quad \underline{\underline{d_1 = 0.3779\lambda}}$$

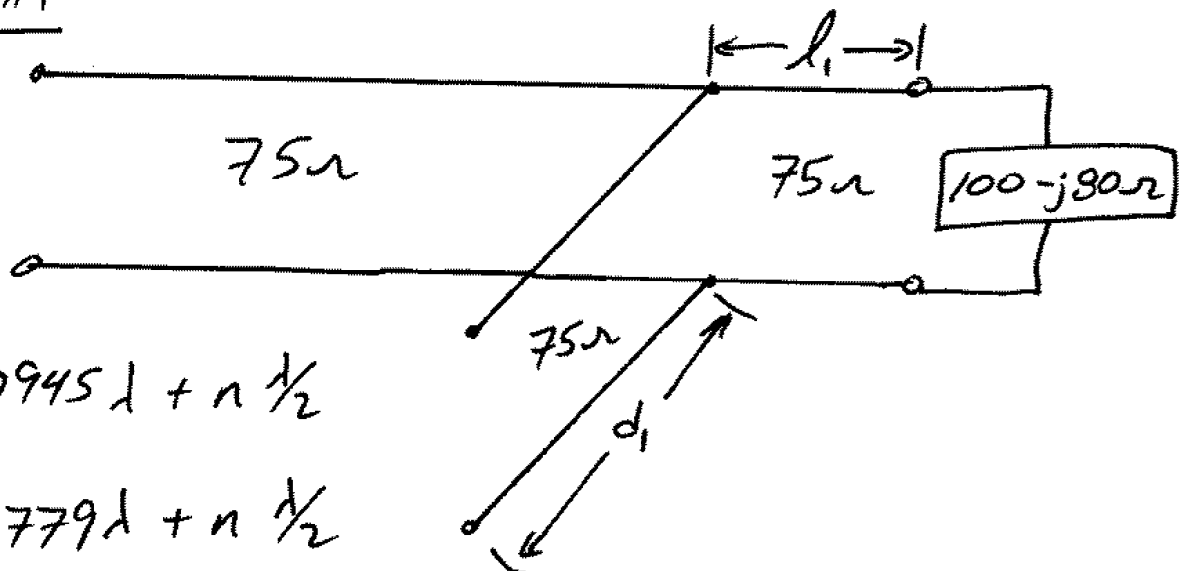
$$\gamma_{\text{stub2}} = +j0.97 \text{ } S/S \quad \underline{\underline{d_2 = 0.1221\lambda}}$$

Find actual stub input admittances

$$y_{\text{stub1}} = -j0.97 \text{ S} \quad Y_{\text{stub1}} = \frac{y_{\text{stub1}}}{z_0} = \underline{\underline{-j12.93 \text{ mS}}}$$

$$y_{\text{stub2}} = +j0.97 \text{ S} \quad Y_{\text{stub2}} = \frac{y_{\text{stub2}}}{z_0} = \underline{\underline{+j12.93 \text{ mS}}}$$

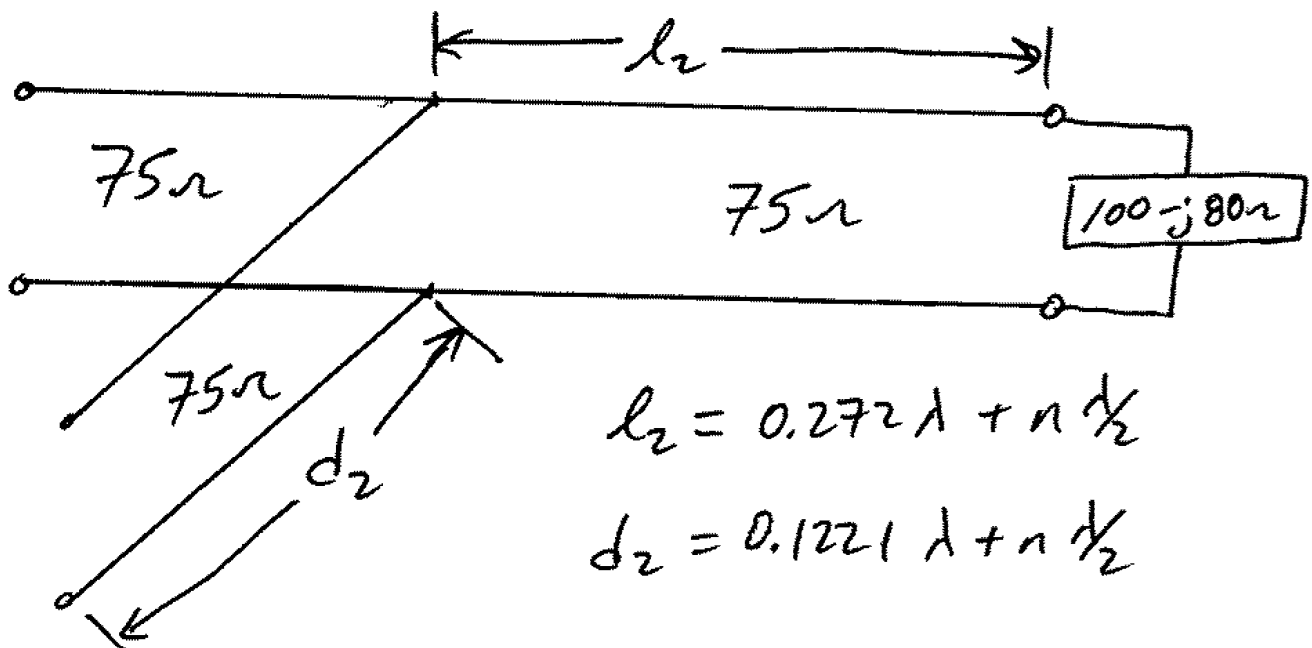
Match #1



$$l_1 = 0.0945 \lambda + n \frac{\lambda}{2}$$

$$d_1 = 0.3779 \lambda + n \frac{\lambda}{2}$$

Match #2



$$l_2 = 0.272 \lambda + n \frac{\lambda}{2}$$

$$d_2 = 0.1221 \lambda + n \frac{\lambda}{2}$$

Simple Smith Chart

$$Z_0 = 75 \Omega$$

