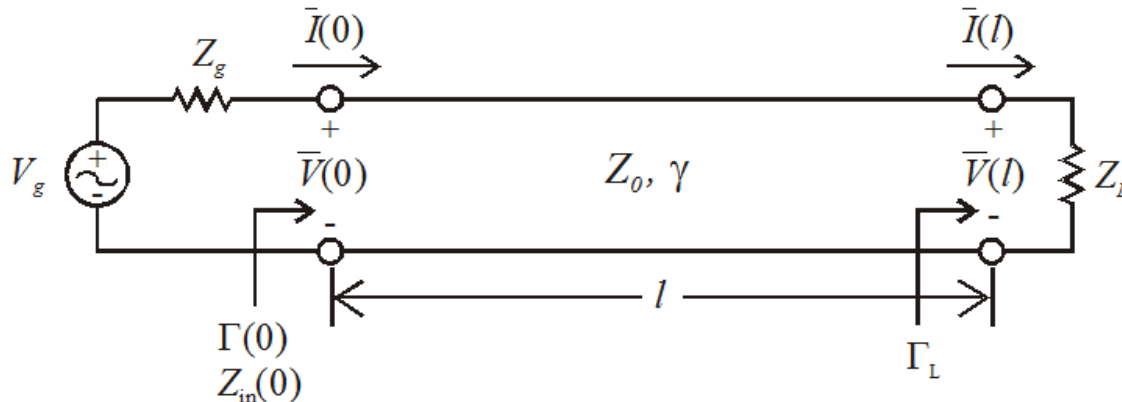


A $45 - j50 \Omega$ load is connected to the end of a 460 cm long lossy transmission line ($\gamma = 0.047 + j 13.88 \text{ m}^{-1}$ and $Z_0 = 54.65 - j 0.1 \Omega$) that is driven by a 400 MHz source where $v_g(t) = 100\cos(\omega t) \text{ V}$ and $Z_g = 50 + j5 \Omega$, determine (a) the input impedance, input reflection coefficient, input voltage, input current, and time-average power delivered to the line. (b) Find the load voltage, load current, and time-average power delivered to the load.



Given:

$$V_g := 100 \cdot e^{j \cdot 0} \text{ V} \quad Z_g := 50 + j \cdot 5 \Omega \quad Z_L := 45 - j \cdot 50 \Omega$$

$$l := 4.6 \text{ m} \quad \gamma := 0.047 + j \cdot 13.88 \text{ 1/m} \quad Z_0 := 54.65 - j \cdot 0.1 \Omega$$

a) Input impedance, reflection coefficient, voltage, current, and time-average power delivered to the line.

$$\Gamma_L := \frac{Z_L - Z_0}{Z_L + Z_0} \quad |\Gamma_L| = 0.45568 \quad \arg(\Gamma_L) \cdot \frac{180}{\pi} = -74.2537 \text{ deg}$$

$$\Gamma_0 := \Gamma_L \cdot e^{-2 \cdot \gamma \cdot l} \quad |\Gamma_0| = 0.29571 \quad \arg(\Gamma_0) \cdot \frac{180}{\pi} = 169.3044 \text{ deg}$$

$$Z_{in0} := Z_0 \cdot \frac{(1 + \Gamma_0)}{(1 - \Gamma_0)} \quad Z_{in0} = 29.89453 + 3.54029i \Omega$$

$$I_0 := \frac{V_g}{Z_g + Z_{in0}} \quad |I_0| = 1.2446 \text{ A} \quad \arg(I_0) \cdot \frac{180}{\pi} = -6.1014 \text{ deg}$$

$$V_0 := \frac{V_g \cdot Z_{in0}}{Z_g + Z_{in0}} \quad |V_0| = 37.4655 \text{ V} \quad \arg(V_0) \cdot \frac{180}{\pi} = 0.6524 \text{ deg}$$

$$\text{Power into trans. line} \quad P_0 := 0.5 \cdot \text{Re}(V_0 \cdot \bar{I}_0) \quad P_0 = 23.15226 \text{ W}$$

b) Load voltage, current, time-average power delivered to the load.

$$V_{0_fwd} := \frac{V_0}{1 + \Gamma_0} \quad V_{0_fwd} = 52.53989 - 3.46321i \text{ V}$$

$$V_L := V_{0_fwd} \cdot e^{-\gamma \cdot l} \cdot (1 + \Gamma_L) \quad |V_L| = 51.1638 \text{ V} \quad \arg(V_L) \cdot \frac{180}{\pi} = -83.314 \text{ deg}$$

$$I_L := \frac{V_{0_fwd}}{Z_0} \cdot e^{-\gamma \cdot l} \cdot (1 - \Gamma_L) \quad |I_L| = 0.7606 \text{ A} \quad \arg(I_L) \cdot \frac{180}{\pi} = -35.301 \text{ deg}$$

$$\text{Power delivered to load-} \quad P_L := 0.5 \cdot \text{Re}(V_L \cdot \bar{I}_L) \quad P_L = 13.0164 \text{ W}$$