

A twin-lead transmission line is made of brass wires with diameters of 1.2 mm, separated by 8 mm center-to-center, embedded in a dielectric insulator characterized by $\epsilon = 1.6\epsilon_0$, $\mu = \mu_0$, and $\sigma = 5 \times 10^{-6} \text{ S/m}$. Determine the skin depth δ and per-unit-length parameters R , L , C , and G at a frequency of 530 MHz.

$$\sigma_{\text{brass}} = 1.1 \times 10^7 \text{ S/m} \text{ per Appendix B}$$

$$\mu_{\text{brass}} = \mu_0, \epsilon_{\text{brass}} = \epsilon_0$$

Use equations from Table 11.1

$$R = \frac{1}{\pi a \delta \sigma_c} \text{ where } \delta = \frac{1}{\sqrt{\pi f \mu_c \sigma_c}}$$

$$\delta = \frac{1}{\sqrt{\pi (530 \times 10^6) (4\pi \times 10^{-7}) (1.1 \times 10^7)}} = \underline{\underline{6.519152 \times 10^{-6} \text{ m}}}$$

$$R = \frac{1}{\pi \left(\frac{1.2 \times 10^{-3}}{2} \right) 6.519152 \times 10^{-6} (1.1 \times 10^7)} = \underline{\underline{7.3168 \, \Omega/\text{m}}}$$

$$L = \frac{\mu}{\pi} \cosh^{-1} \left(\frac{d}{2a} \right) = \frac{4\pi \times 10^{-7}}{\pi} \cosh^{-1} \left(\frac{8}{1.2} \right)$$

$$L = \underline{\underline{1.0338 \times 10^{-6} \text{ H/m} = 1.034 \, \mu\text{H/m}}}$$

$$G = \frac{\pi \sigma}{\cosh^{-1}(d/2a)} = \frac{\pi (5 \times 10^{-6})}{\cosh^{-1}(8/1.2)} = 6.0775 \times 10^{-6} \text{ S/m}$$

$$\underline{\underline{G = 6.0775 \, \mu\text{S/m}}}$$

$$C = \frac{\pi \epsilon}{\cosh^{-1}(d/2a)} = \frac{\pi (8.8542 \times 10^{-12}) 1.6}{\cosh^{-1}(8/1.2)} = 1.722 \times 10^{-11} \text{ F/m}$$

$$\underline{\underline{C = 17.22 \text{ pF/m}}}$$