

11.52 A $50\ \Omega$ air-filled line is terminated in a mismatched load of $40 + j25\ \Omega$. Find the shortest distance from the load at which the voltage has the smallest magnitude.

- Use Smith chart. Also, find the load reflection coefficient, SWR, and shortest distance from the load to where the voltage has the largest magnitude. Distances are in terms of λ .
- Calculate the normalized load impedance $z_L = Z_L / Z_0 = (40 + j25) / 50$
 $\Rightarrow z_L = 0.8 + j0.5\ \Omega/\Omega$. Plot z_L on Smith chart.
- Use compass to draw a circle through z_L , centered on Smith chart. Use a straight edge to draw radial line from center of Smith chart through z_L to outer rings of Smith chart.
- Move in the “WAVELENGTHS TOWARD GENERATOR” direction on the circle of constant $|\Gamma|$ from z_L point at 0.1163 to r_{\min} point/ V_{\min} point at 0.5. Shortest distance from load to V_{\min} point is $d_{V_{\min}} / \lambda = 0.5 - 0.1163 \Rightarrow d_{V_{\min}} = 0.3837\lambda$.
- Use the “ANGLE OF REFLECTION COEFFICIENT IN DEGREES” scale to read $\angle \Gamma_L = 96.3^\circ$.
- Use compass (same setting) to mark the “SWR (VSWR)” and “REFL. COEFF, V or I” scales. Read off $|\Gamma| = 0.29$ and $\Rightarrow \text{SWR} = 1.81$.
- Put the magnitude and angle of the load reflection coefficient together to get $\Rightarrow \Gamma = \Gamma_L = 0.29 \angle 96.3^\circ$.
- Last, move in the “WAVELENGTHS TOWARD GENERATOR” direction on the circle of constant $|\Gamma|$ from z_L point @ 0.1163 to r_{\max} point/ V_{\max} point @ 0.25. The shortest distance from load to V_{\max} is $d_{V_{\max}} / \lambda = 0.25 - 0.1163 \Rightarrow d_{V_{\max}} = 0.1337\lambda$.

Simple Smith Chart

 $0.1163, 96.3^\circ$ $Z_0 = 50 \Omega$ λ unspecified