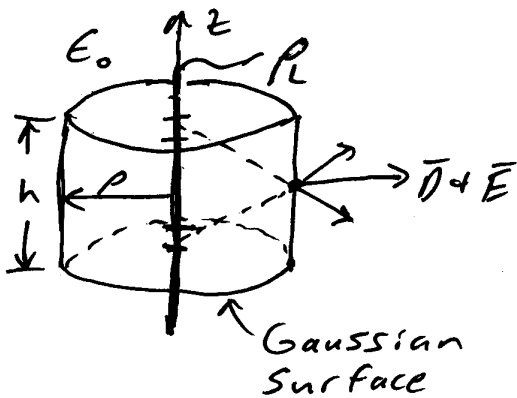


**Example-** Using Gauss' Law, find the electric flux density and electric field vectors due to an infinite uniform line charge on the z-axis in free space.



\* By symmetry, we expect  $\vec{D}$  &  $\vec{E}$  to only have  $\rho$ -components  
 \* At a fixed radial distance from the z-axis, we expect  $|\vec{D}| = \text{constant}$  &  $|\vec{E}| = \text{constant}$

Based on these observations, choose a cylinder of radius  $\rho$  and height  $h$ , concentric w/ the z-axis as the Gaussian surface.

$$\text{Gauss' Law } \oiint_S \vec{D} \cdot d\vec{S} = Q_{\text{enc}}$$

$$\iint_{\text{Top}} \hat{a}_\rho D_\rho \cdot d\vec{S}_z + \iint_{\text{Bottom}} \hat{a}_\rho D_\rho \cdot (-d\vec{S}_z) + \iint_{\text{Side}} \hat{a}_\rho D_\rho \cdot d\vec{S}_\rho = \rho_L h$$

$$D_\rho \iint_{\text{Side}} dS_\rho = D_\rho (2\pi\rho h) = \rho_L h$$

$$\hookrightarrow D_\rho = \frac{\rho_L}{2\pi\rho}$$

$$\vec{D} = \hat{a}_\rho \frac{\rho_L}{2\pi\rho} \quad \rho > 0$$

$$\vec{E} = \vec{D}/\epsilon_0 = \hat{a}_\rho \frac{\rho_L}{2\pi\epsilon_0\rho} \quad \rho > 0$$

What if we have a uniform line charge NOT on the z-axis?  $\rho_L$   $\times$   $\vec{D} + \vec{E}$ ?

$$\vec{D} = \hat{a}_R \frac{\rho_L}{2\pi R} \quad R > 0$$

$$\vec{E} = \hat{a}_R \frac{\rho_L}{2\pi R} \quad R > 0$$

$\vec{R}$  is radial vector normally out from line charge.