

**Example-** Illustrate forward and backward wave propagation  
lossy transmission line (Belden 9085).

**From earlier example**

$$f := 100 \cdot 10^6 \quad \text{Hz} \qquad \omega := 2 \cdot \pi \cdot f \qquad \omega = 6.283 \times 10^8 \quad \text{rad/s}$$

$$\underline{R} := 6.21118 \quad \Omega/\text{m} \qquad \underline{L} := 1.25311 \cdot 10^{-6} \quad \text{H/m}$$

$$\underline{G} := 1.3538 \cdot 10^{-5} \quad \text{S/m} \qquad \underline{C} := 1.39135 \cdot 10^{-11} \quad \text{F/m}$$

**Calculate a few parameters**

**Propagation constant (11.11)**

$$\gamma := \sqrt{(R + j \cdot \omega \cdot L) \cdot (G + j \cdot \omega \cdot C)} \qquad \boxed{\gamma = 0.01238 + 2.62358i} \quad 1/\text{m}$$

**Attenuation constant**       $\alpha := \text{Re}(\gamma)$        $\boxed{\alpha = 0.01238}$       Np/m

$$\alpha_{\text{dB}} := 20 \cdot \log(\exp(\alpha)) \qquad \boxed{\alpha_{\text{dB}} = 0.1075} \quad \text{dB/m}$$

**Phase constant**       $\beta := \text{Im}(\gamma)$        $\boxed{\beta = 2.62358}$       rad/m

**Wavelength (11.13)**       $\lambda := \frac{2 \cdot \pi}{\beta}$        $\boxed{\lambda = 2.39489}$       m

**Phase velocity (11.14)**       $u := \frac{\omega}{\beta}$        $\boxed{u = 2.39489 \times 10^8}$       m/s

**Characteristic Impedance (11.19)**       $Z_0 := \sqrt{\frac{R + j \cdot \omega \cdot L}{G + j \cdot \omega \cdot C}}$        $\boxed{Z_0 = 300.11017 - 0.95134i}$        $\Omega$

**Define some constants for the forward & backward propagating voltage waves**

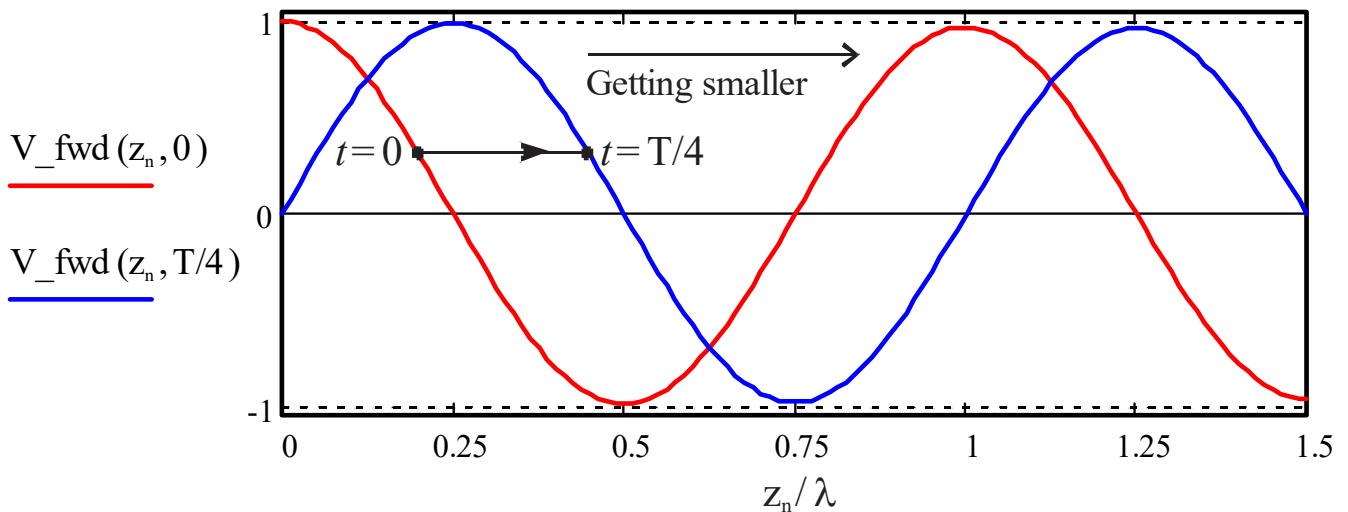
$$V_{\text{plus}} := 1 \quad \text{V} \quad V_{\text{minus}} := 1 \quad \text{V} \quad T := \frac{2\pi}{\omega} \quad T = 1 \times 10^{-8} \quad \text{s}$$

**Define functions for forward and backward components of the voltage wave**

$$V_{\text{fwd}}(z, t) := V_{\text{plus}} \cdot e^{-\alpha \cdot z} \cdot \cos(\omega \cdot t - \beta \cdot z) \quad n := 0..120 \quad z_n := \frac{1.5 \cdot \lambda \cdot n}{120}$$

$$V_{\text{bwd}}(z, t) := V_{\text{minus}} \cdot e^{\alpha \cdot z} \cdot \cos(\omega \cdot t + \beta \cdot z)$$

**Forward Traveling Voltage wave**



**Backward Traveling Voltage wave**

