

Example- Illustrate forward and backward wave propagation for a lossless transmission line (based on Belden 9085).

From earlier example

$$\begin{array}{llll}
 f := 100 \cdot 10^6 & \text{Hz} & \omega := 2 \cdot \pi \cdot f & \omega = 6.283 \times 10^8 \quad \text{rad/s} \\
 \underline{R} := 0 & \Omega/\text{m} & \underline{L} := 1.25311 \cdot 10^{-6} & \text{H/m} \\
 \underline{G} := 0 & \text{S/m} & \underline{C} := 1.39135 \cdot 10^{-11} & \text{F/m}
 \end{array}$$

Calculate a few parameters

Propagation constant (11.11)/(11.21a)

$$\gamma := \sqrt{(R + j \cdot \omega \cdot L) \cdot (G + j \cdot \omega \cdot C)} \quad \boxed{\gamma = 2.62357i} \quad 1/\text{m}$$

Attenuation constant $\alpha := 0$ $\boxed{\alpha = 0}$ Np/m

$$\alpha_{\text{dB}} := 20 \cdot \log(\exp(\alpha)) \quad \boxed{\alpha_{\text{dB}} = 0} \quad \text{dB/m}$$

Phase constant (11.21a) $\beta := \omega \cdot \sqrt{L \cdot C}$ $\boxed{\beta = 2.62357}$ rad/m

Wavelength (11.13) $\lambda := \frac{2 \cdot \pi}{\beta}$ $\boxed{\lambda = 2.3949}$ m

Phase velocity (11.21b) $u := \frac{1}{\sqrt{L \cdot C}}$ $\boxed{u = 2.3949 \times 10^8}$ m/s

Characteristic Impedance (11.21c) $Z_0 := \sqrt{\frac{L}{C}}$ $\boxed{Z_0 = 300.10719}$ Ω

Note: Most of these parameters changed very little from the lossy case. This makes sense as the Belden 9085 twin-lead is very lowloss at 100 MHz.

Define some constants for the forward & backward propagating voltage waves

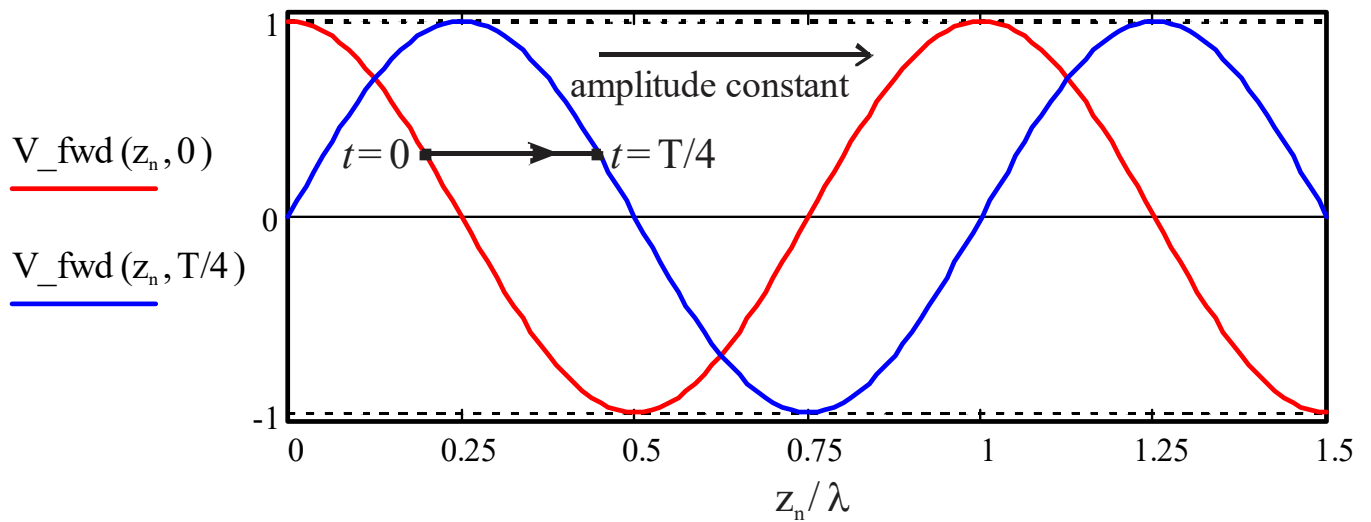
$$V_{\text{plus}} := 1 \quad \text{V} \quad V_{\text{minus}} := 1 \quad \text{V} \quad T := \frac{2\pi}{\omega} \quad T = 1 \times 10^{-8} \quad \text{s}$$

Define functions for forward and backward components of the voltage wave

$$V_{\text{fwd}}(z, t) := V_{\text{plus}} \cdot \cos(\omega \cdot t - \beta \cdot z) \quad n := 0..120 \quad z_n := \frac{1.5 \cdot \lambda \cdot n}{120}$$

$$V_{\text{bwd}}(z, t) := V_{\text{minus}} \cdot \cos(\omega \cdot t + \beta \cdot z)$$

Forward Traveling Voltage wave



Backward Traveling Voltage wave

