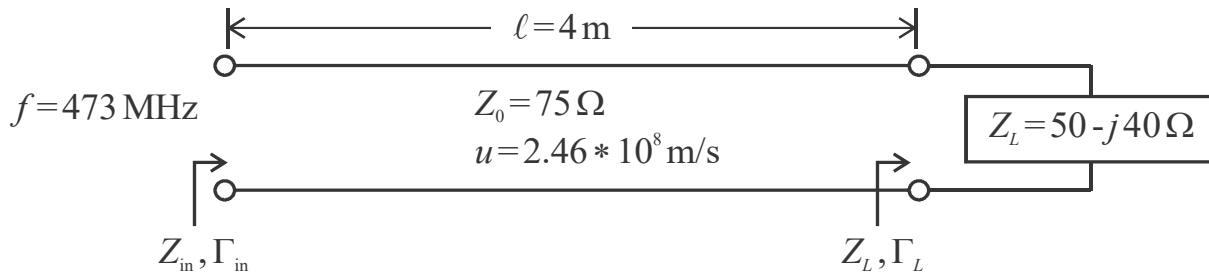


At 473 MHz, a load has an impedance of $50 - j40$ Ohms. If it is attached to a lossless transmission line (similar to RG-6) where $Z_0 = 75$ Ohms, $u = 2.46 \times 10^8$ m/s, & $l = 4$ m, calculate phase constant, wavelength, electrical length, reflection coefficients at the input and load ends of the transmission line, input impedance, and standing wave ratio.



Given: $f := 473 \cdot 10^6$ Hz $L := 4$ m $u := 2.46 \cdot 10^8$ m/s
 $Z_0 := 75$ Ω $Z_L := 50 - j \cdot 40$ Ω

Calculate phase constant β , wavelength λ , and electrical length βL :

$$\beta := \frac{2 \cdot \pi \cdot f}{u} \quad \boxed{\beta = 12.081} \text{ rad/m}$$

$$\lambda := \frac{u}{f} \quad \boxed{\lambda = 0.5201} \text{ m}$$

$$\beta L := \beta \cdot L \quad \boxed{\beta L = 48.324} \text{ rad} \quad \boxed{\beta L \cdot \frac{180}{\pi} = 2768.8} \text{ deg} \quad \boxed{\frac{\beta L}{2 \cdot \pi} = 7.691} \lambda$$

Calculate reflection coefficients at input Γ_{in} and load Γ_L :

$$\Gamma_L := \frac{Z_L - Z_0}{Z_L + Z_0} \quad \boxed{|\Gamma_L| = 0.3594} \quad \boxed{\arg(\Gamma_L) \cdot \frac{180}{\pi} = -104.261} \text{ deg}$$

$$\Gamma_{in} := \Gamma_L \cdot e^{-j \cdot 2 \cdot \beta \cdot L} \quad \boxed{|\Gamma_{in}| = 0.3594} \quad \boxed{\arg(\Gamma_{in}) \cdot \frac{180}{\pi} = 118.178} \text{ deg}$$

Calculate input impedance and standing wave ratio:

$$Z_{in} := Z_0 \cdot \frac{(1 + \Gamma_{in})}{1 - \Gamma_{in}} \quad \boxed{Z_{in} = 44.472 + 32.358i} \Omega$$

$$S := \frac{(1 + |\Gamma_{in}|)}{(1 - |\Gamma_{in}|)} \quad \boxed{S = 2.122} \quad \text{VSWR} := \frac{1 + |\Gamma_L|}{1 - |\Gamma_L|} \quad \boxed{\text{VSWR} = 2.122}$$