

EE 362 Electronic, Magnetic, & Optical Properties of Materials

Quiz 6 (Spring 2024)

Name Key A

Instructions: Open book & notes. Place answers in indicated spaces. Show all work. Use 4-5 significant figures.

At 300 K, a section of gallium arsenide has been uniformly doped exclusively with acceptor atoms to a concentration of $5 \times 10^{13} \text{#/cm}^3$. First, find the majority & minority carrier concentrations (#/cm^3), majority & minority carrier mobilities ($\text{cm}^2/\text{V}\cdot\text{s}$), and majority & minority diffusion coefficients (cm^2/s). Then, determine the ambipolar carrier mobility ($\text{cm}^2/\text{V}\cdot\text{s}$) and diffusion coefficient (cm^2/s).

$$N_a = 5 \times 10^{13} \frac{\#}{\text{cm}^3} \quad \text{From Table B.4, } n_i = 1.8 \times 10^6 \frac{\#}{\text{cm}^3} \\ @ 300 \text{K for GaAs}$$

$$\text{majority carriers} = p_0 \approx N_a = \underline{5 \times 10^{13} \frac{\#}{\text{cm}^3}} \quad \text{can confirm w (4.62)}$$

$$(4.43) n_0 p_0 = n_i^2 \Rightarrow n_0 = \frac{(1.8 \times 10^6)^2}{5 \times 10^{13}} = \underline{0.0648 \frac{\#}{\text{cm}^3}} \\ \text{minority carriers}$$

As $N_a = 5 \times 10^{13} \frac{\#}{\text{cm}^3} < 10^{14} \text{cm}^{-3}$ on graph, use

Table 5.1 to get $\underline{M_n = 8500 \frac{\text{cm}^2}{\text{V}\cdot\text{s}}}$ (minority)
 mobilities

$\underline{M_p = 400 \frac{\text{cm}^2}{\text{V}\cdot\text{s}}}$ (majority)

Per Einstein relation (5.47)

$$\frac{D_n}{M_n} = \frac{D_p}{M_p} = \frac{k_B T}{e} = \frac{(8.617333 \times 10^{-5} \text{eV/K}) 300 \text{K}}{e} = 0.025852 \checkmark$$

$$D_n = 8500(0.025852) = \underline{219.742 \frac{\text{cm}^2}{\text{s}}} \quad \text{minority}$$

$$D_p = 400(0.025852) = \underline{10.3408 \frac{\text{cm}^2}{\text{s}}} \quad \text{majority}$$

Since $p_0 \gg n_0$ (p -type)

$$(6.45) \underline{D' = D_n = 219.742 \frac{\text{cm}^2}{\text{s}}} \quad + (6.46) \underline{M' = M_n = 8500 \frac{\text{cm}^2}{\text{V}\cdot\text{s}}}$$

$$\rho_0 = \text{majority carrier conc.} = 5 \times 10^{13} \frac{\#}{\text{cm}^3}$$

$$\text{minority carrier conc.} = 0.0698 \frac{\#}{\text{cm}^3}$$

$$\text{majority carrier mobility} = \mu_p = 400 \frac{\text{cm}^2}{\text{V-s}}$$

$$\text{minority carrier mobility} = \mu_n = 8500 \frac{\text{cm}^2}{\text{V-s}}$$

$$\text{majority diffusion coeff.} = D_p = 10.341 \frac{\text{cm}^2}{\text{s}}$$

$$\text{minority diffusion coeff.} = D_n = 219.742 \frac{\text{cm}^2}{\text{s}}$$

$$\text{ambipolar carrier mobility} = \mu' = 8500 \frac{\text{cm}^2}{\text{s}}$$

$$\text{ambipolar diffusion coeff.} = D' = 219.742 \frac{\text{cm}^2}{\text{s}}$$

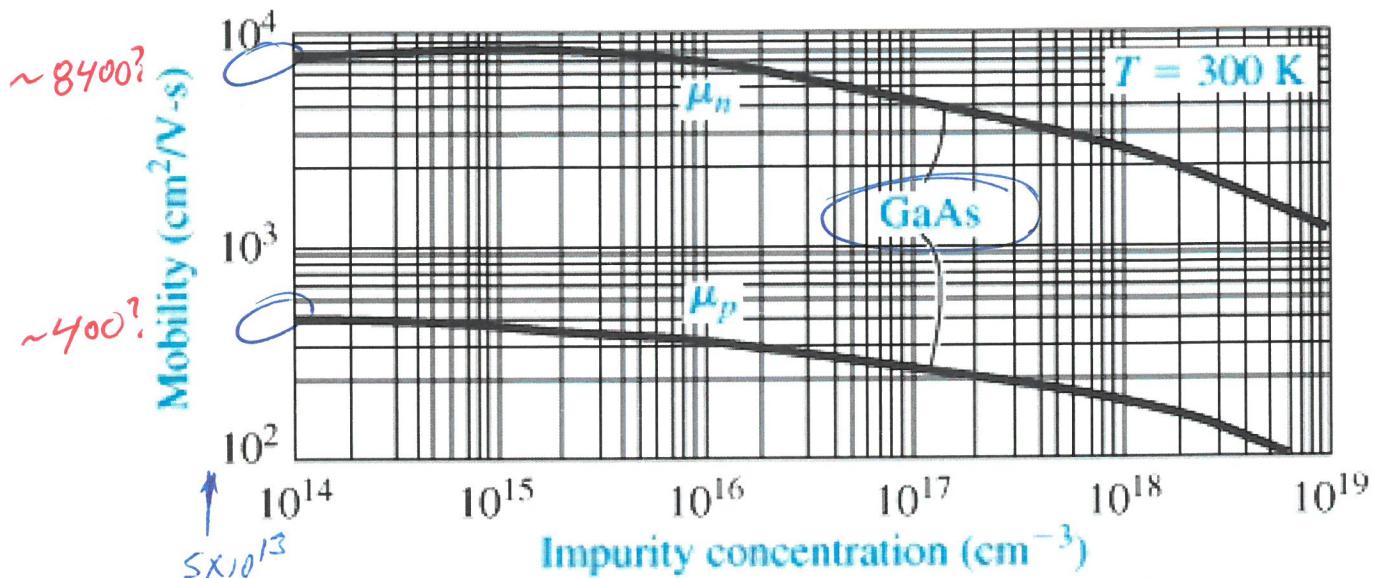
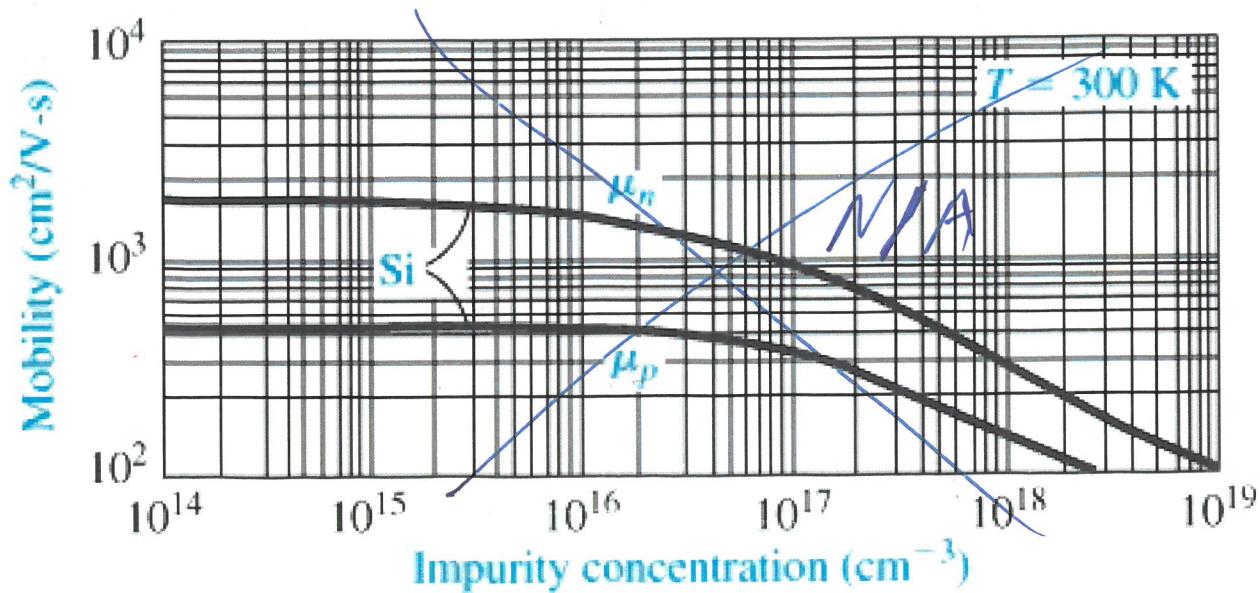


Table 5.1 | Typical mobility values at $T = 300 \text{ K}$ and low doping concentrations

	μ_n ($\text{cm}^2/\text{V}\cdot\text{s}$)	μ_p ($\text{cm}^2/\text{V}\cdot\text{s}$)
Silicon	1350	480
Gallium arsenide	8500	400
Germanium	3900	1900

use



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Quiz 6 (Spring 2024)

Name Key C

Instructions: Open book & notes. Place answers in indicated spaces. Show all work. Use 4-5 significant figures.

At 300 K, a section of silicon has been uniformly doped exclusively with donor atoms to a concentration of $2 \times 10^{14} \text{#/cm}^3$. First, find the majority & minority carrier concentrations (#/cm^3), majority & minority carrier mobilities ($\text{cm}^2/\text{V}\cdot\text{s}$), and majority & minority diffusion coefficients (cm^2/s). Then, determine the ambipolar carrier mobility ($\text{cm}^2/\text{V}\cdot\text{s}$) and diffusion coefficient (cm^2/s).

$$N_d = 2 \times 10^{14} \frac{\#}{\text{cm}^3} \quad \text{From Table B.4, } n_i = 1.5 \times 10^{10} \frac{\#}{\text{cm}^3} \\ @ 300 \text{K for Si}$$

$$\text{majority carriers} = n_o = N_d = 2 \times 10^{14} \frac{\#}{\text{cm}^3} \quad \text{can confirm w/ (4.60)}$$

$$(4.43) n_o p_o = n_i^2 \Rightarrow p_o = \frac{(1.5 \times 10^{10})^2}{2 \times 10^{14}} = \frac{1.125 \times 10^6}{\text{minority carriers}} \frac{\#}{\text{cm}^3}$$

use either Si graph or Table 5.1 to get

$$\text{mobilities } \mu_n = 1350 \frac{\text{cm}^2}{\text{V}\cdot\text{s}} \quad (\text{majority})$$

$$\mu_p = 480 \frac{\text{cm}^2}{\text{V}\cdot\text{s}} \quad (\text{minority})$$

Per Einstein relation (5.47)

$$\frac{D_n}{\mu_n} = \frac{D_p}{\mu_p} = \frac{k_B T}{e} = 8.617333 \times 10^{-5} (300) = 0.025852 \text{ V}$$

$$D_n = 1350 (0.025852) = \underline{34.9002 \frac{\text{cm}^2}{\text{s}}} \quad (\text{majority})$$

$$D_p = 480 (0.025852) = \underline{12.40896 \frac{\text{cm}^2}{\text{s}}} \quad (\text{minority})$$

Since $n_o \gg p_o$ (n-type)

$$(6.47) D' = D_p = \underline{12.409 \frac{\text{cm}^2}{\text{s}}} \quad \text{and} \quad (6.48) \mu' = -\mu_p = -480 \frac{\text{cm}^2}{\text{V}\cdot\text{s}}$$

$$n_0 = \text{majority carrier conc.} = 2 \times 10^{14} \frac{\#}{\text{cm}^3}$$

$$\rho_0 = \text{minority carrier conc.} = 1.125 \times 10^6 \frac{\#}{\text{cm}^3}$$

$$\text{majority carrier mobility} = \mu_n = 1350 \frac{\text{cm}^2}{\text{V}\cdot\text{s}}$$

$$\text{minority carrier mobility} = \mu_p = 480 \frac{\text{cm}^2}{\text{V}\cdot\text{s}}$$

$$\text{majority diffusion coeff.} = D_n = 34.9 \frac{\text{cm}^2}{\text{s}}$$

$$\text{minority diffusion coeff.} = D_p = 12.409 \frac{\text{cm}^2}{\text{s}}$$

$$\mu' = \text{ambipolar carrier mobility} = -480 \frac{\text{cm}^2}{\text{V}\cdot\text{s}}$$

$$D' = \text{ambipolar diffusion coeff.} = 12.409 \frac{\text{cm}^2}{\text{s}}$$

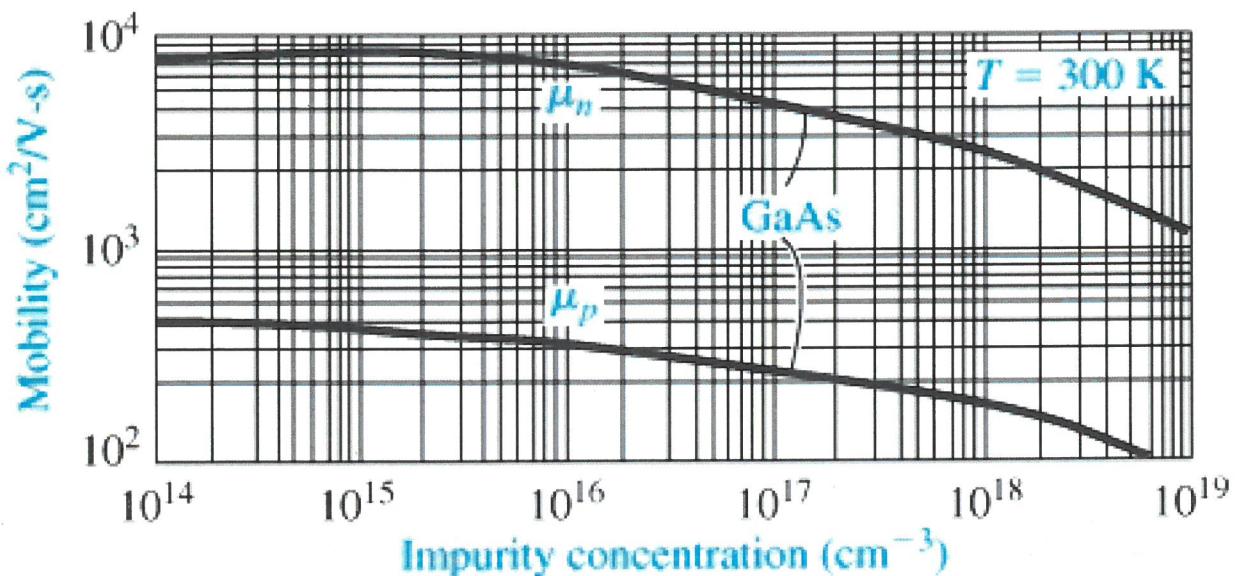


Table 5.1 | Typical mobility values at $T = 300 \text{ K}$ and low doping concentrations

	$\mu_n (\text{cm}^2/\text{V}\cdot\text{s})$	$\mu_p (\text{cm}^2/\text{V}\cdot\text{s})$
Silicon	1350	480
Gallium arsenide	8500	400
Germanium	3900	1900

use \rightarrow

