

EE 362 Electronic, Magnetic, & Optical Properties of Materials

Quiz 3 (Spring 2024)

Name Key A

Instructions: Open book & notes. Place answers in indicated spaces. Show all work. Use 4-5 significant figures.

A tin selenide (SnSe) semiconductor has a bandgap of 0.9 eV. At 325 K, assume the Fermi energy level is at midgap. First, find $k_B T$ (eV). Then, calculate the energy difference $\Delta E_1 = E_c + 0.6k_B T - E_F$ (eV). Finally, determine the probability that a state at energy $E_F + \Delta E_1$ is occupied by an **electron** (unitless).

$$k_B T = (8.617333 \times 10^{-5} \frac{\text{eV}}{\text{K}})(325 \text{ K}) = \underline{0.028006 \text{ eV}}$$

$$\begin{aligned} \Delta E_1 &= E_c - E_F + 0.6 k_B T = E_c - \left(\frac{E_c + E_V}{2} \right) + 0.6 k_B T \\ &= \frac{E_c}{2} - \frac{E_V}{2} + 0.6 k_B T \quad \text{but } E_g = E_c - E_V \\ &= \frac{E_g}{2} + 0.6 k_B T = \frac{0.9}{2} + 0.6(0.028006) \\ &= \underline{0.466804 \text{ eV}} \end{aligned}$$

$$(3.79) \quad f_F(E) = \frac{1}{1 + e^{(E - E_F)/k_B T}}$$

$$\text{Where } E - E_F = (E_F + \Delta E_1) - E_F = \Delta E_1$$

$$\begin{aligned} f_F(E_F + \Delta E_1) &= \frac{1}{1 + e^{0.466804/0.028006}} \approx e^{\frac{-0.466804}{0.028006}} \\ &= \underline{5.77123 \times 10^{-8}} \quad (\text{M-B approx}) \end{aligned}$$

$$k_B T = \underline{0.028006 \text{ eV}} \quad \Delta E_1 = \underline{0.466804 \text{ eV}} \quad \text{prob}_{e,\Delta E_1} = \underline{5.7712 \times 10^{-8}}$$

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Name Key B

Instructions: Open book & notes. Place answers in indicated spaces. Show all work. Use 4-5 significant figures.

A magnesium silicide (Mg_2Si) semiconductor has a bandgap of 0.79 eV. At 275 K, the Fermi energy level is at midgap. First, find $k_B T$ (eV). Then, calculate the energy difference $\Delta E_2 = E_c + 0.3k_B T - E_F$ (eV). Finally, determine the probability that a state at energy $E_F + \Delta E_2$ is occupied by an **electron** (unitless).

$$k_B T = (8.617333 \times 10^{-5} \frac{\text{eV}}{\text{K}})(275\text{K}) = \underline{0.023698 \text{ eV}}$$

$$\begin{aligned} \Delta E_2 &= E_c - E_F + 0.3k_B T = E_c - \left(\frac{E_c + E_V}{2}\right) + 0.3k_B T \\ &= \frac{E_c}{2} - \frac{E_V}{2} + 0.3k_B T \quad \text{midgap} \\ &\quad \text{where } E_g = E_c - E_V \\ &= \frac{E_g}{2} + 0.3k_B T = \frac{0.79}{2} + 0.3(0.023698) \end{aligned}$$

$$\underline{\Delta E_2 = 0.402109 \text{ eV}}$$

$$(3.79) \quad f_F(E) = \frac{1}{1 + e^{(E - E_F)/k_B T}}$$

$$\text{where } E - E_F = (E_F + \Delta E_2) - E_F = \Delta E_2$$

$$\begin{aligned} f_F(E_F + \Delta E_2) &= \frac{1}{1 + e^{0.402109/0.023698}} \approx e^{-0.402109/0.023698} \\ &= \underline{4.27324 \times 10^{-8}} \quad (\text{m-B approx.}) \end{aligned}$$

$$k_B T = \underline{0.023698 \text{ eV}} \quad \Delta E_2 = \underline{0.40211 \text{ eV}} \quad \text{prob}_{e,\Delta E_2} = \underline{4.2732 \times 10^{-8}}$$