

4.1 Calculate the intrinsic carrier concentration, n_i , at $T = 200, 400,$ and 600 K for (c) gallium arsenide.

> Also, find $N_c, N_v,$ and $k_B T$ at each temperature.

From Table B.4, $E_g = 1.42$ eV, $m_n^* = 0.067 m_0$, & $m_p^* = 0.48 m_0$

$$\begin{aligned} \underline{200\text{ K}} \quad k_B T &= 8.617333 \times 10^{-5} (200) = 0.017235 \text{ eV} \\ &= 1.38065 \times 10^{-23} (200) = 2.7613 \times 10^{-21} \text{ J} \end{aligned}$$

$$(4.10) \quad N_c = 2 \left(\frac{2\pi m_n^* k_B T}{h^2} \right)^{3/2}$$

$$N_c = 2 \left[\frac{2\pi (0.067)(9.1093837 \times 10^{-31}) (1.380649 \times 10^{-23})}{(6.62607 \times 10^{-34})^2} \right]^{3/2} 200^{3/2}$$

$$= 8.37534 \times 10^{19} (200)^{3/2} \Rightarrow$$

$$\begin{aligned} N_c &= 2.3689 \times 10^{23} \frac{\#}{\text{m}^3} \\ &= 2.3689 \times 10^{17} \frac{\#}{\text{cm}^3} \end{aligned}$$

$$(4.10) \quad N_v = 2 \left(\frac{2\pi m_p^* k_B T}{h^2} \right)^{3/2}$$

$$N_v = 2 \left[\frac{2\pi (0.48)(9.1093837 \times 10^{-31}) (1.380649 \times 10^{-23})}{(6.62607 \times 10^{-34})^2} \right]^{3/2} 200^{3/2}$$

$$= 1.60602 \times 10^{21} (200)^{3/2} \Rightarrow$$

$$\begin{aligned} N_v &= 4.5425 \times 10^{24} \frac{\#}{\text{m}^3} \\ &= 4.5425 \times 10^{18} \frac{\#}{\text{cm}^3} \end{aligned}$$

$$(4.23) \quad n_i^2 = N_c N_v e^{-E_g/k_B T}$$

$$n_i^2 = 2.3689 \times 10^{23} (4.5425 \times 10^{24}) e^{-\frac{1.42}{0.017235}}$$

$$= 1.7759 \times 10^{12}$$

$$n_i = \sqrt{1.7759 \times 10^{12}} = 1.3326 \times 10^6 \frac{\#}{\text{m}^3} = 1.3326 \frac{\#}{\text{cm}^3}$$

$$\begin{aligned} \underline{400\text{K}} \quad k_B T &= 2(2.7613 \times 10^{-21}) = \underline{5.5226 \times 10^{-21} \text{ J}} \\ &= 2(0.017235) = \underline{0.034469 \text{ eV}} \end{aligned}$$

$$N_c = 8.37534 \times 10^{19} (400)^{3/2}$$

$$\underline{N_c = 6.7003 \times 10^{23} \#/\text{m}^3 = 6.7003 \times 10^{17} \#/\text{cm}^3}$$

$$N_v = 1.60602 \times 10^{21} (400)^{3/2}$$

$$\underline{N_v = 1.2848 \times 10^{25} \#/\text{m}^3 = 1.2848 \times 10^{19} \#/\text{cm}^3}$$

$$\begin{aligned} n_i^2 &= 6.7003 \times 10^{23} (1.2848 \times 10^{25}) e^{\frac{-1.42}{0.034469}} \\ &= 1.1059 \times 10^{31} \end{aligned}$$

$$\underline{n_i = 3.3255 \times 10^{15} \#/\text{m}^3 = 3.3255 \times 10^9 \#/\text{cm}^3}$$

$$\begin{aligned} \underline{600\text{K}} \quad k_B T &= 3(2.27613 \times 10^{-21}) = \underline{8.2839 \times 10^{-21} \text{ J}} \\ &= 3(0.017235) = \underline{0.051704 \text{ eV}} \end{aligned}$$

$$N_c = 8.37534 \times 10^{19} (600)^{3/2}$$

$$\underline{N_c = 1.2309 \times 10^{24} \#/\text{m}^3 = 1.2309 \times 10^{18} \#/\text{cm}^3}$$

$$N_v = 1.60602 \times 10^{21} (600)^{3/2}$$

$$\underline{N_v = 2.3604 \times 10^{25} \#/\text{m}^3 = 2.3604 \times 10^{19} \#/\text{cm}^3}$$

$$\begin{aligned} n_i^2 &= (1.2309 \times 10^{24}) (2.3604 \times 10^{25}) e^{\frac{-1.42}{0.051704}} \\ &= 3.4335 \times 10^{37} \end{aligned}$$

$$\underline{n_i = 5.8596 \times 10^{18} \#/\text{m}^3 = 5.8596 \times 10^{12} \#/\text{cm}^3}$$