

**3.26** (a) Determine the total number (#/cm<sup>3</sup>) of energy states in silicon between  $E_c$  and  $E_c + 2kT$  at (i)  $T = 300$  K and (ii)  $T = 400$  K.

➤ Repeat part a) for Germanium.

c) Per (3.72),  $g_c(E) = \frac{4\pi(2m_n^*)^{3/2}}{h^3} \sqrt{E - E_c}$ . Then following Example 3.4, the number of conduction energy states in Germanium between  $E_c$  and  $E_c + 2k_B T$  is

$$\begin{aligned} N_c &= \int_{E_c}^{E_c+2k_B T} g_c(E) dE = \int_{E_c}^{E_c+2k_B T} \frac{4\pi(2m_n^*)^{3/2}}{h^3} \sqrt{E - E_c} dE \\ &= \left[ \frac{4\pi(2m_n^*)^{3/2}}{h^3} \frac{2}{3} (E - E_c)^{3/2} \right]_{E_c}^{E_c+2k_B T} = \frac{8\pi(2m_n^*)^{3/2}}{3h^3} \left[ (E_c + 2k_B T - E_c)^{3/2} - (E_c - E_c)^{3/2} \right] \\ &= \frac{8\pi(2m_n^*)^{3/2}}{3h^3} (2k_B T)^{3/2} \end{aligned}$$

Per Table B.4, the density of states effective electron mass for Germanium is  $m_n^* = 0.55m_0$ . Using this value and other constants, we get

$$\begin{aligned} N_c &= \frac{8\pi \left( 2(0.55)9.1093837 \times 10^{-31} \right)^{3/2}}{3 \left( 6.62607015 \times 10^{-34} \right)^3} \left[ 2(1.380649 \times 10^{-23}) \right]^{3/2} T^{3/2} \\ &= 1.667643 \times 10^{20} T^{3/2} \end{aligned}$$

(i) At  $T = 300$  K,  $N_c = 1.667643 \times 10^{20} (300)^{3/2}$

$$\Rightarrow \underline{N_c = 8.66533 \times 10^{23} \text{ \#/m}^3 = 8.66533 \times 10^{17} \text{ \#/cm}^3}.$$

(ii) At  $T = 400$  K,  $N_c = 1.667643 \times 10^{20} (400)^{3/2}$

$$\Rightarrow \underline{N_c = 1.33411 \times 10^{24} \text{ \#/m}^3 = 1.33411 \times 10^{18} \text{ \#/cm}^3}.$$