

Example- For an AC motor, we measure the line voltage to be 120 V_{RMS} and the line current to be 12 A_{RMS} using a multimeter while the power is measured to be 1150 W using a wattmeter. Determine the apparent power, power factor, complex power, reactive power, and load impedance. [Hint: Motors are resistive-inductive loads.]

Time-average Real Power (given): $\Rightarrow \underline{P = 1150 \text{ W}}$

Apparent Power: $S = VI = 120(12) \Rightarrow \underline{S = 1440 \text{ VA}}$

Power Factor: $PF = P/S = 1150/1440 \Rightarrow \underline{PF = 0.7986 \text{ lagging (RL load)}}$

Complex Power:

$$\theta_Z = \theta_S = \cos^{-1}(PF) = \cos^{-1}(0.7986) \Rightarrow \underline{\theta_S = +37.002^\circ \text{ (RL load)}}$$

$$\bar{S} = S \angle \theta_S \Rightarrow \underline{\bar{S} = 1440 \angle 37.002^\circ \text{ VA}} \Rightarrow \underline{\bar{S} = 1150 + j866.66 \text{ VA}}$$

Reactive Power: $Q = \text{Im}(\bar{S}) = \text{Im}(1150 + j866.66) \Rightarrow \underline{Q = 866.66 \text{ var}}$

Load Impedance:

$$Z = V/I = 120/12 = \underline{10 \Omega}$$

$$\theta_Z = \theta_S = \cos^{-1}(PF) = \cos^{-1}(0.7986) = \underline{+37.002^\circ \text{ (RL load)}}$$

$$\bar{Z} = Z \angle \theta_Z \Rightarrow \underline{\bar{Z} = 10 \angle 37.002^\circ \Omega} \Rightarrow \underline{\bar{Z} = 7.986 + j6.018 \Omega}$$