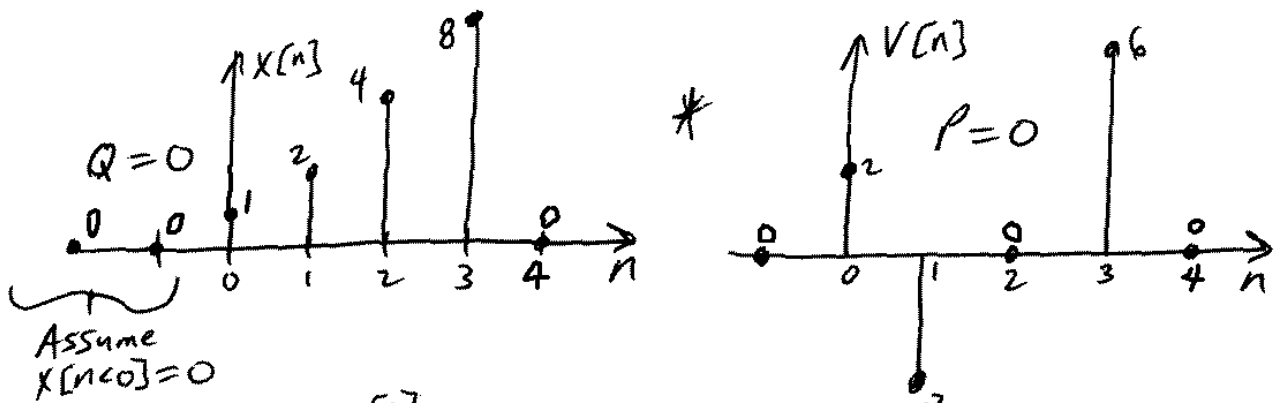


**2.8** For the discrete-time signals  $x[n]$  and  $v[n]$  given in each of the following parts, compute the convolution  $x[n] * v[n]$  for  $n \geq 0$

- (c)  $x[n] = 2^n$  for  $n \leq 3$  and  $x[n] = 0$  for  $n \geq 4$ ;  $v[0] = 2, v[1] = -3, v[2] = 0, v[3] = 6, v[n] = 0$  for all other integers  $n$ .



Hand-drawn convolution table:

		$x[0]$	1	2	4	8
$v[0] \rightarrow 2$			2	4	8	16
$-3$			-3	-6	-12	-24
$0$			0	0	0	0
$6$			6	12	24	48

$$P + Q = 0 + 0 = 0$$

Let  $y[n] = x[n] * v[n]$

$$y[0] = 2$$

$$y[1] = -3 + 4 = 1$$

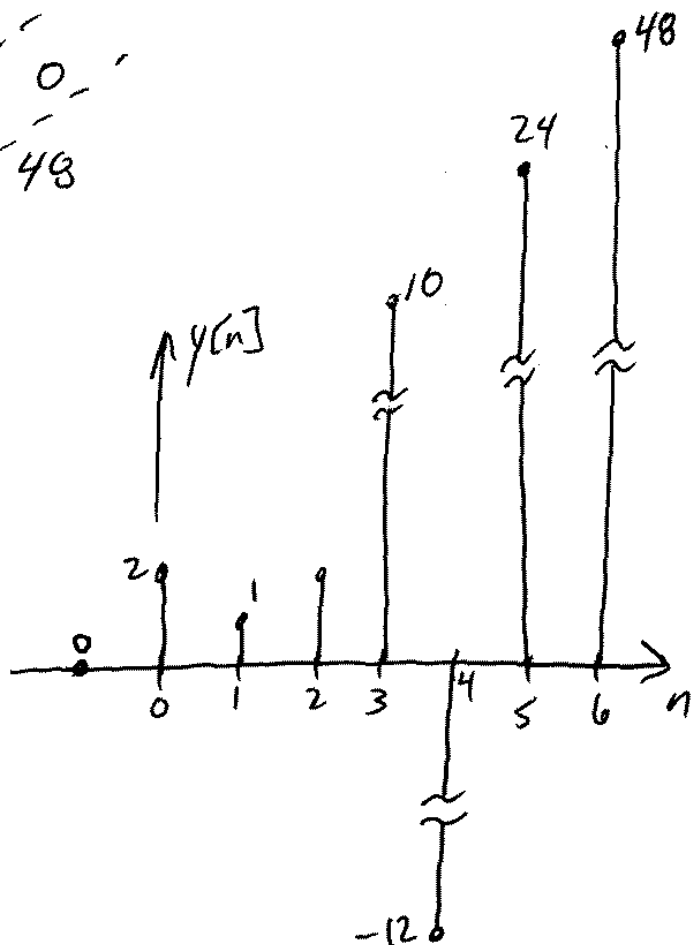
$$y[2] = 0 - 6 + 8 = 2$$

$$y[3] = 6 + 0 - 12 + 16 = 10$$

$$y[4] = 12 - 24 = -12$$

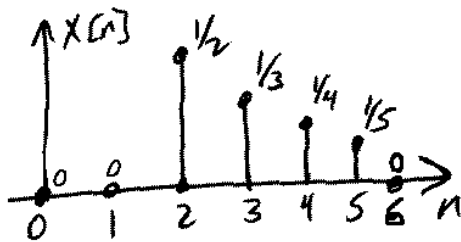
$$y[5] = 24 + 0 = 24$$

$$y[6] = 48$$

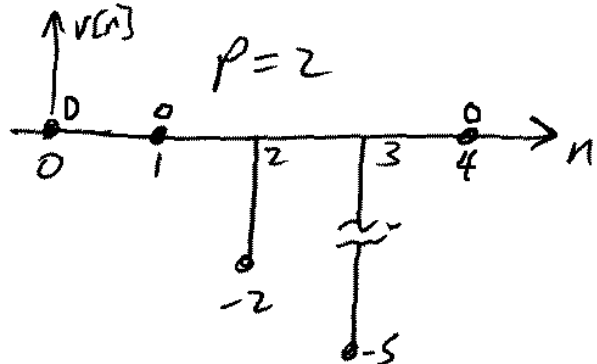


**2.8** For the discrete-time signals  $x[n]$  and  $v[n]$  given in each of the following parts, compute the convolution  $x[n] * v[n]$  for  $n \geq 0$

- (d)  $x[n] = 1/n$  for  $2 \leq n \leq 5$  and  $x[n] = 0$  for all other integers  $n$ ;  $v[2] = -2$ ,  $v[3] = -5$ ,  $v[n] = 0$  for all other integers  $n$ .



$$Q=2$$



$$P=2$$

$$\begin{array}{r} \frac{1}{2} \quad \frac{1}{3} \quad \frac{1}{4} \quad \frac{1}{5} \\ -2 \left[ \begin{array}{cccc} -1 & -2/3 & -1/2 & -2/5 \\ -5/2 & -5/3 & -5/4 & -1 \end{array} \right] \\ -5 \end{array}$$

$$P+Q=2+2=4$$

$$y[4] = -1$$

$$y[5] = -5/2 - 2/3 = -3.1\bar{6}$$

$$y[6] = -5/3 - 1/2 = -2.1\bar{6}$$

$$y[7] = -5/4 - 2/5 = -1.65$$

$$y[8] = -1$$

$$y[n < 4 + n > 8] = 0$$

