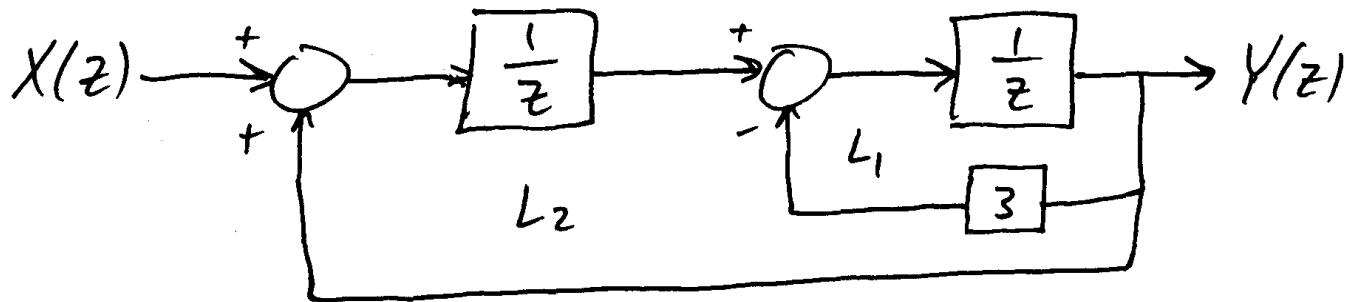


Example- Find the system transfer function $H(z)$ using Mason's Theorem.



Only one forward path $P_1(z) = \frac{1}{z} \left(\frac{1}{z} \right) = \frac{1}{z^2}$

$$\text{Loop 1 } L_1(z) = \frac{1}{z} (3)(-1) = -\frac{3}{z}$$

$$\text{Loop 2 } L_2(z) = \frac{1}{z} \left(\frac{1}{z} \right)(1) = \frac{1}{z^2}$$

Note, $L_1(z)$ and $L_2(z)$ touch. Forward path $P_1(z)$ touches both $L_1(z)$ & $L_2(z)$.

System determinant is then

$$\begin{aligned} D(z) &= 1 - \sum_{i=1}^2 L_i(z) + 0 \text{ on touching} \\ &= 1 - [L_1(z) + L_2(z)] \\ &= 1 + \frac{3}{z} - \frac{1}{z^2} \end{aligned}$$

$$H(z) = \frac{\sum_{i=1}^r P_i(z) D_i(z)}{D(z)} = \frac{P_1(z) D_1(z)}{D(z)}$$

and

$D_1(z) = 1$ since both loops touch $P_1(z)$

$$H(z) = \frac{1/z^2(1)}{1 + 3/z - 1/z^2}$$

$$\underline{H(z) = \frac{1}{z^2 + 3z - 1}} \Rightarrow \text{Same answer!}$$