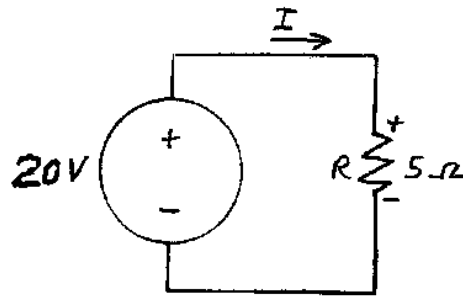


2.2

For this circuit:

a) Find power, P , absorbed by resistor.

$$\begin{aligned} P &= \frac{V^2}{R} \\ &= \frac{(20V)^2}{5\Omega} \\ &= \underline{\underline{80 \text{ Watts}}} \end{aligned}$$

b) Find a value of R such that the absorbed power doubles.

$$\begin{aligned} P &= 160W \quad V = 20V \\ P &= \frac{V^2}{R} \\ R &= \frac{V^2}{P} \\ &= \frac{(20V)^2}{160W} \\ &= \underline{\underline{2.50\Omega}} \end{aligned}$$

c) Find a value for the source voltage to restore P to 80W.

$$\begin{aligned} P &= 80W \quad R = 2.50\Omega \\ P &= \frac{V^2}{R} \\ V^2 &= PR \\ V &= \sqrt{PR} \\ &= \sqrt{(80W)(2.50\Omega)} \\ &= \underline{\underline{14.1V}} \end{aligned}$$

2.3 The dc resistance of a conductor is:

$$R = \frac{\rho l}{A} = \frac{l}{\sigma A}$$

ρ = electrical resistivity (Ωm)

l = length of conductor (m)

A = cross-sectional area (m^2)

σ = electrical conductivity ($\frac{\text{S}}{\text{m}}$)

- a) Find the resistance and voltage of a copper bus bar 1 by 5cm in cross section and 30cm long when carrying a current of 250 A.

Compute cross section area.

$$\begin{aligned} A &= (1\text{cm})(5\text{cm}) \\ &= 5\text{cm}^2 \\ &= \underline{\underline{0.0005\text{m}^2}} \end{aligned}$$

Compute resistance. For copper $\sigma = 5.8 \times 10^7 \text{ S/m}$

$$\begin{aligned} R &= \frac{l}{\sigma A} \\ &= \frac{(30\text{cm})(\frac{1\text{m}}{100\text{cm}})}{(5.8 \times 10^7 \frac{\text{S}}{\text{m}})(0.0005\text{m}^2)} \\ &= \underline{\underline{1.03 \times 10^{-5} \Omega}} \end{aligned}$$

Compute voltage.

$$\begin{aligned} V &= IR \\ &= (250\text{A})(1.03 \times 10^{-5} \Omega) \\ &= \underline{\underline{2.58 \times 10^{-3} \text{V}}} \end{aligned}$$

- b) An aluminum conductor 50 Km long has a circular cross section with a diameter of 1cm.

Find power absorbed by wire when carrying 100 A.

Compute cross section area.

$$\begin{aligned} A &= \pi r^2 \\ &= (\pi)(0.5\text{cm})^2 \\ &= 7.85 \times 10^{-1} \text{cm}^2 \\ &= \underline{\underline{7.85 \times 10^{-5} \text{m}^2}} \end{aligned}$$

2.3b cont.) Compute resistance

For aluminum $\sigma = 3.5 \times 10^7 \frac{S}{m}$

$$\begin{aligned}
 R &= \frac{l}{\sigma A} \\
 &= \frac{(50 \text{ km}) \left(\frac{1000 \text{ m}}{\text{km}} \right)}{\left(3.5 \times 10^7 \frac{S}{m} \right) \left(7.85 \times 10^{-5} \text{ m}^2 \right)} \\
 &= \underline{\underline{18.2 \Omega}}
 \end{aligned}$$

Compute power absorbed

$$P = I^2 R$$

$$\begin{aligned}
 P &= (100 \text{ A})^2 (18.2 \Omega) \\
 &= \underline{\underline{1.82 \times 10^5 \text{ W}}}
 \end{aligned}$$

- c) Let us assume that one of Edison's light bulbs was a 30W model connected to a 36V battery. The carbon filament had a diameter of 0.2mm. Find the length of the filament in inches assuming the resistivity of carbon to be twice its room temperature value when in use.

Compute resistance.

$$\begin{aligned}
 P &= \frac{V^2}{R} \\
 R &= \frac{V^2}{P} \\
 &= \frac{(36 \text{ V})^2}{30 \text{ W}} \\
 &= \underline{\underline{43.2 \Omega}}
 \end{aligned}$$

Compute cross section area.

$$R = 0.2 \text{ mm} = 2 \times 10^{-4} \text{ m}$$

$$\begin{aligned}
 A &= \pi R^2 \\
 &= (\pi) (2 \times 10^{-4} \text{ m})^2 \\
 &= \underline{\underline{1.26 \times 10^{-7} \text{ m}^2}}
 \end{aligned}$$

Compute length of filament

$$\text{carbon's } \sigma = 2.9 \times 10^4 \frac{S}{m}$$

$$\begin{aligned}
 R &= \frac{l}{\sigma A} \\
 l &= R \sigma A \\
 &= (43.2 \Omega) \left(2.9 \times 10^4 \frac{S}{m} \right) \left(1.26 \times 10^{-7} \text{ m}^2 \right) \\
 &= (0.316 \text{ m}) \left(\frac{39.37 \text{ in}}{1 \text{ m}} \right) \\
 &= \underline{\underline{12.4 \text{ inches}}}
 \end{aligned}$$